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# Computer Graphics Hardware Pipeline

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*Visual Imaging  
in the Electronic Age*

Prof. Donald P. Greenberg

October 22, 2020

Lecture 15

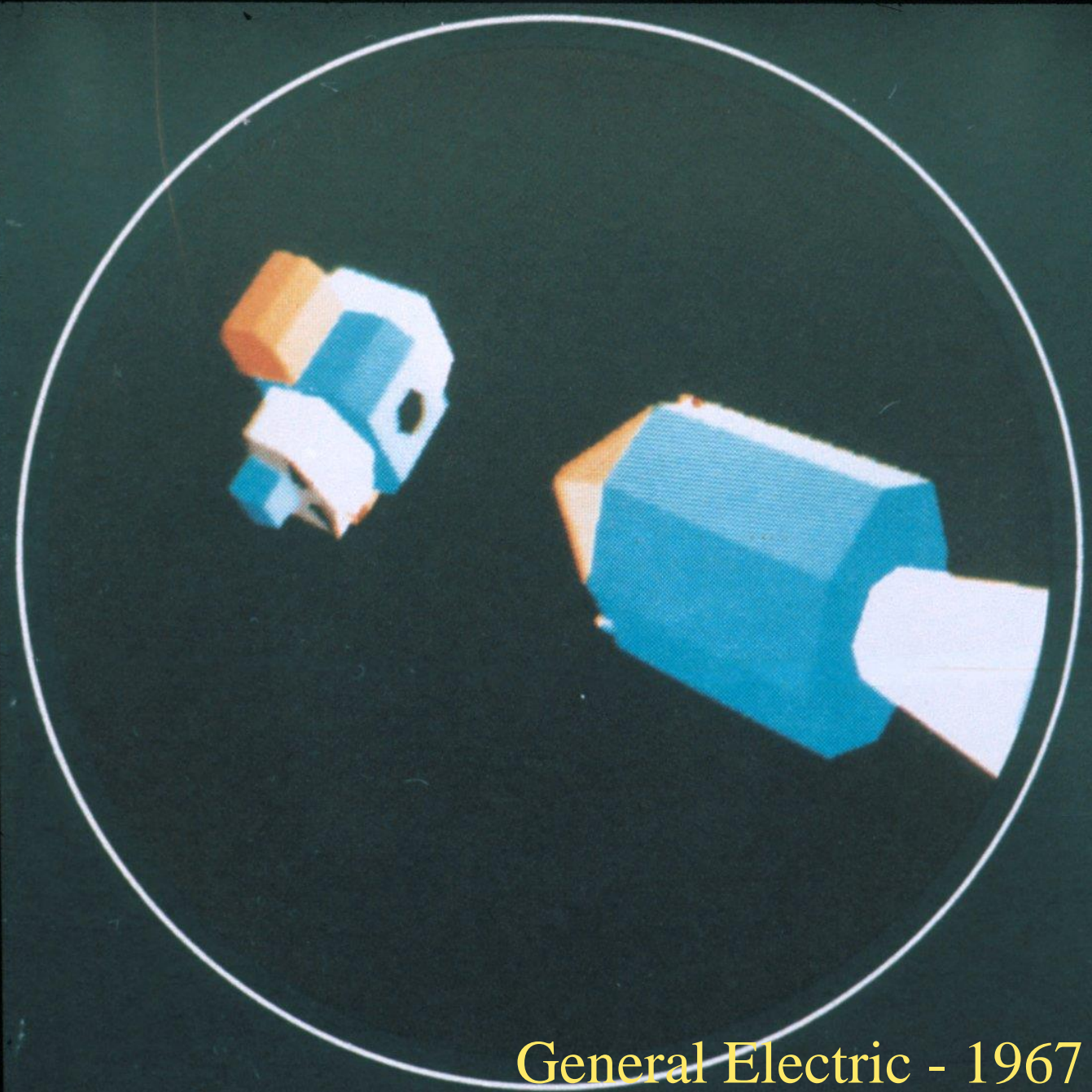
# Moore's Law

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*“Chip density doubles every 18 months.”*

Processing Power (P) in 15 years:

$$\begin{aligned} P &= P_{today} (2)^{\frac{15 \text{ years}}{18 \text{ months}}} = P_t (2)^{\frac{15}{1.5}} \\ &= P_t (2)^{10} = 1000 P_t \end{aligned}$$



General Electric - 1967

# Xerox Sigma 5

1965-7



- Cost: \$300,000
- 16K Magnetic memory

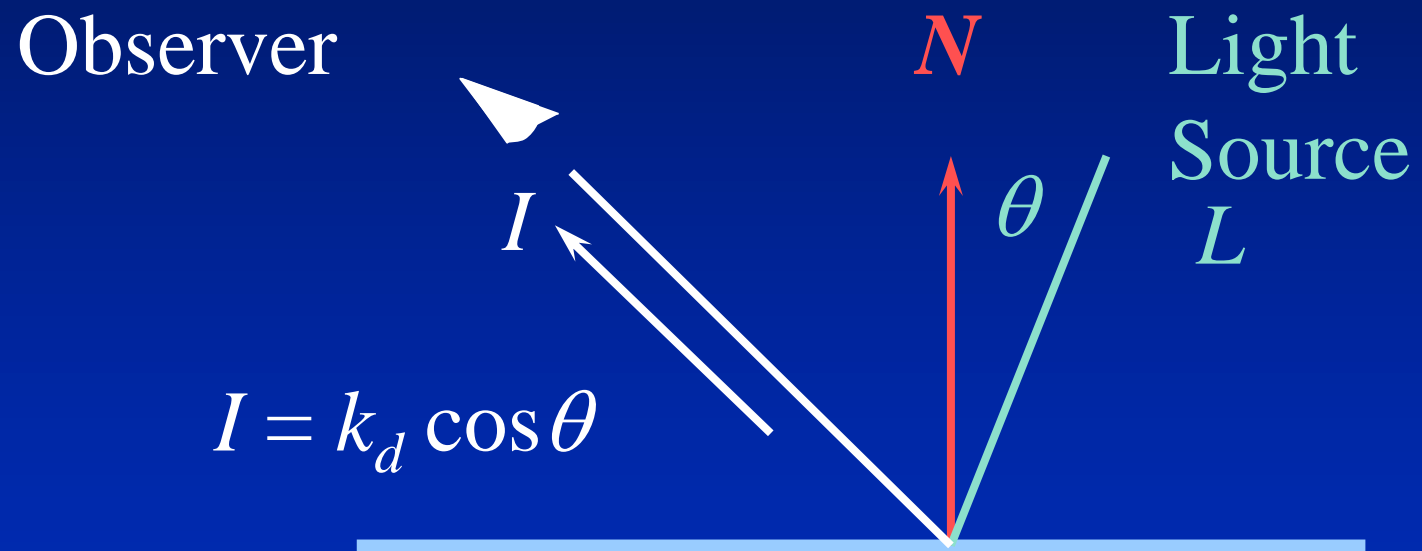
# Cornell in Perspective Film



# Direct Illumination

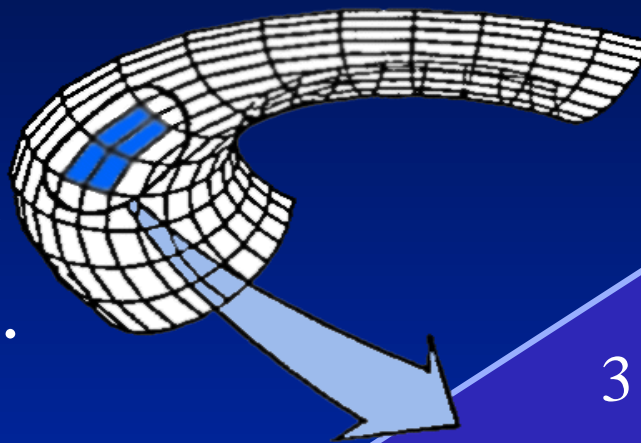


# Diffuse Reflections



# Gouraud Smooth Shading

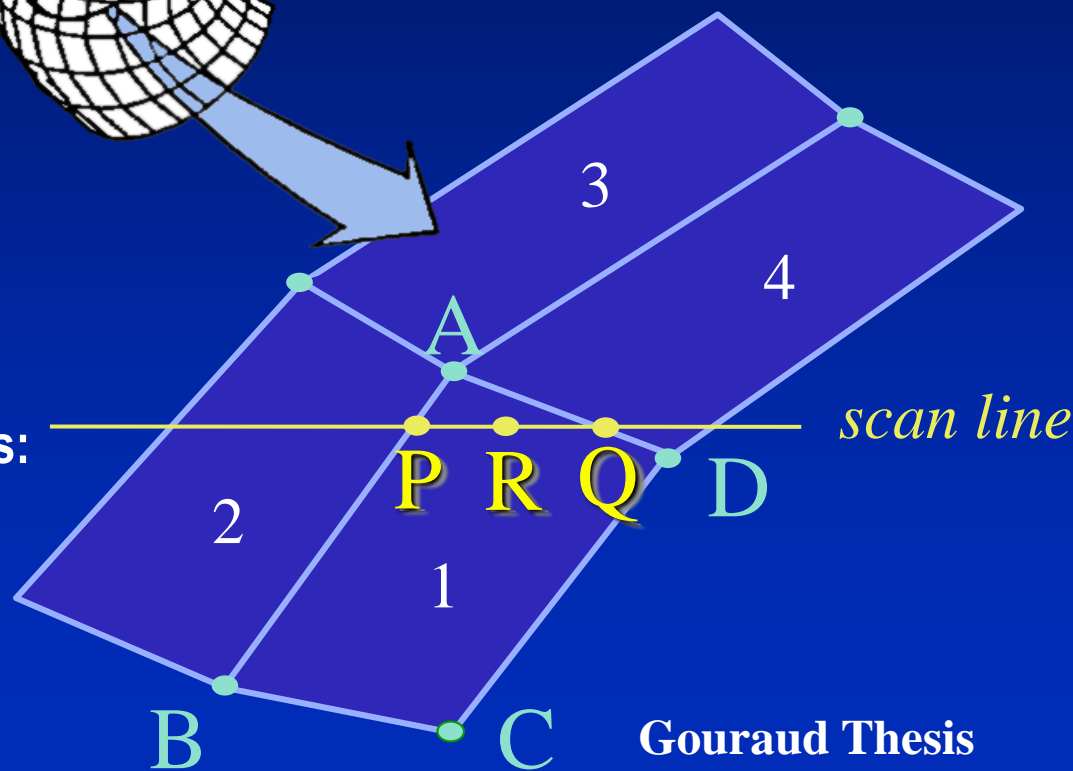
Four polygons approximating a surface in the vicinity of point A.



The shading at point R is computed as two types of successive linear interpolations:

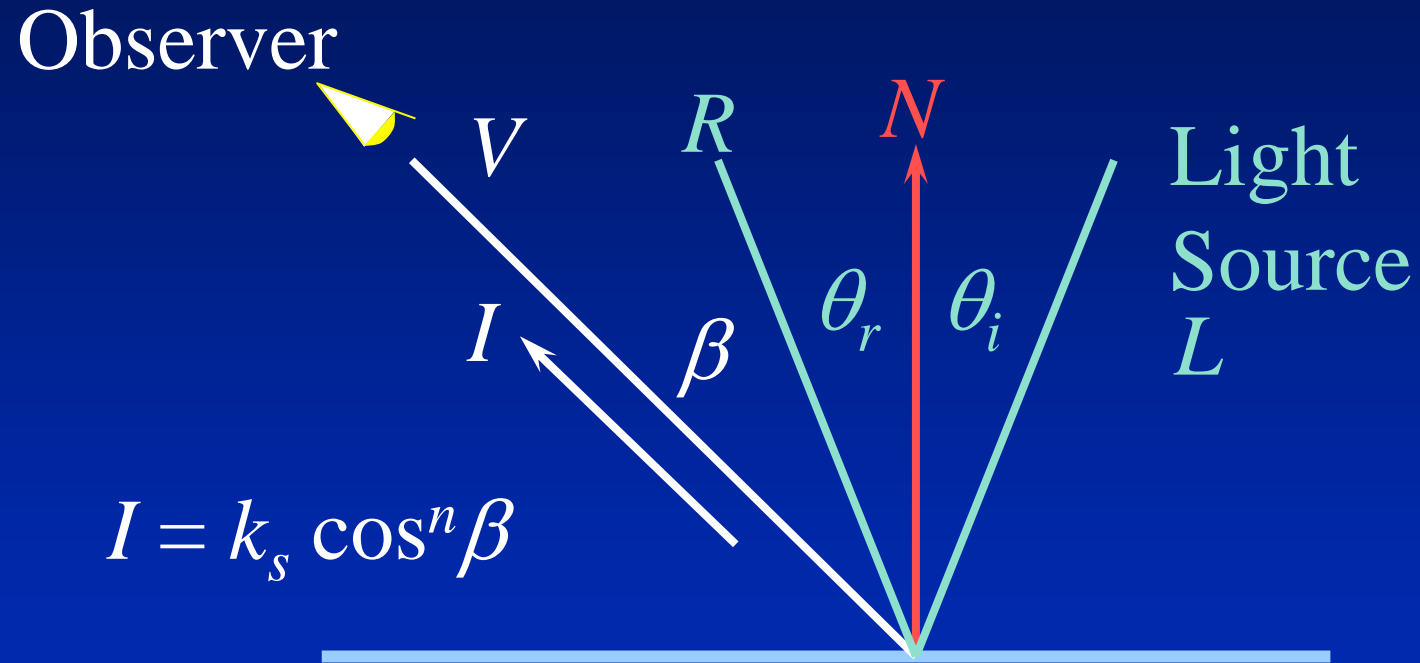
across polygon edges: P between A and B,  
Q between A and D;

across the scan line: R between P and Q.





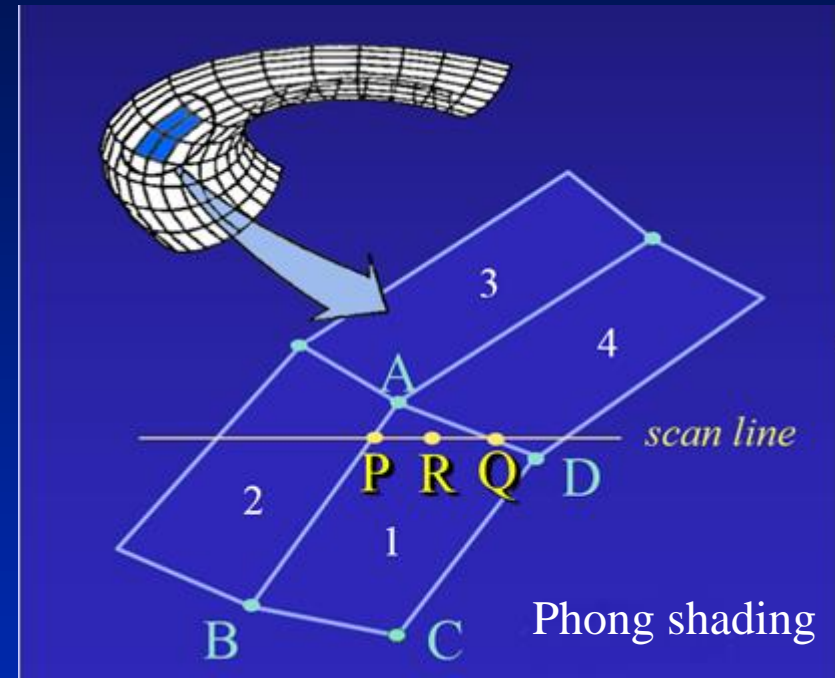
# Phong Model Specular Reflection





# Phong Smooth Shading

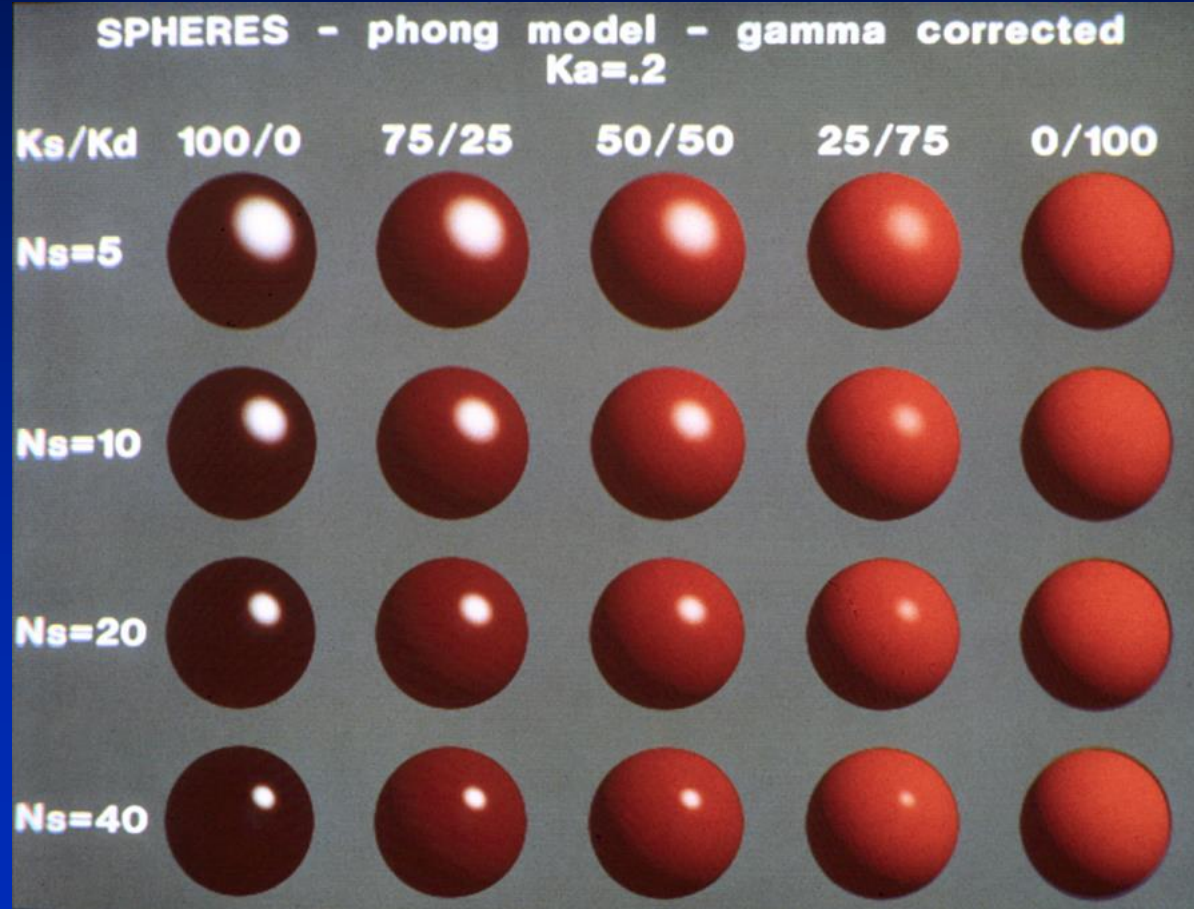
Four polygons  
approximating a surface  
in the vicinity of point A.  
The shading at point R is computed as  
two types of successive linear interpolations:  
two types of successive linear interpolations:  
across polygon edges: P between A and B,  
Q between A and D;  
across the scan line: R between P and Q.



The only difference between Gouraud and Phong shading is that the colors at A, B, C, and D need to be computed to include the specular reflections.

# Direct Lighting

# Phong Reflection Model



# End of Review

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# Digital Equipment PDP 11/45

1973

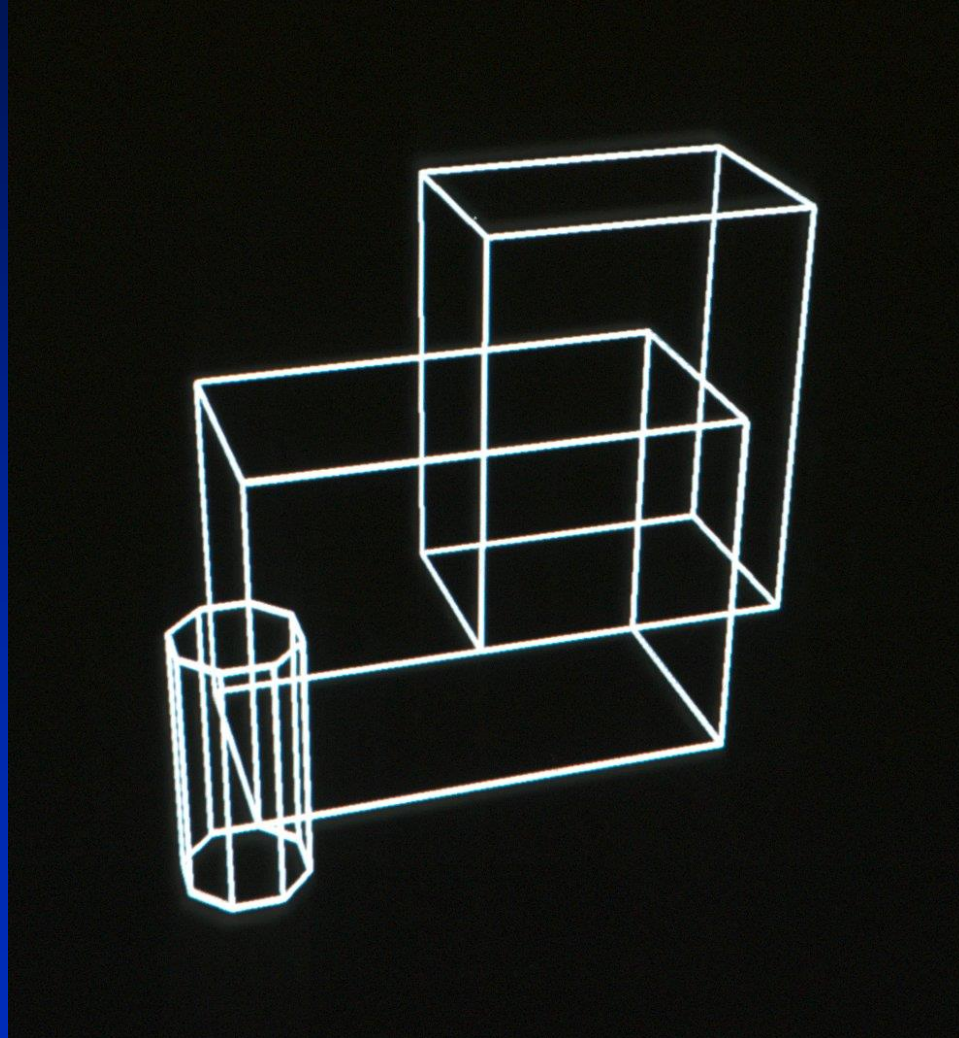


- Cost:



# Hidden Line Algorithm

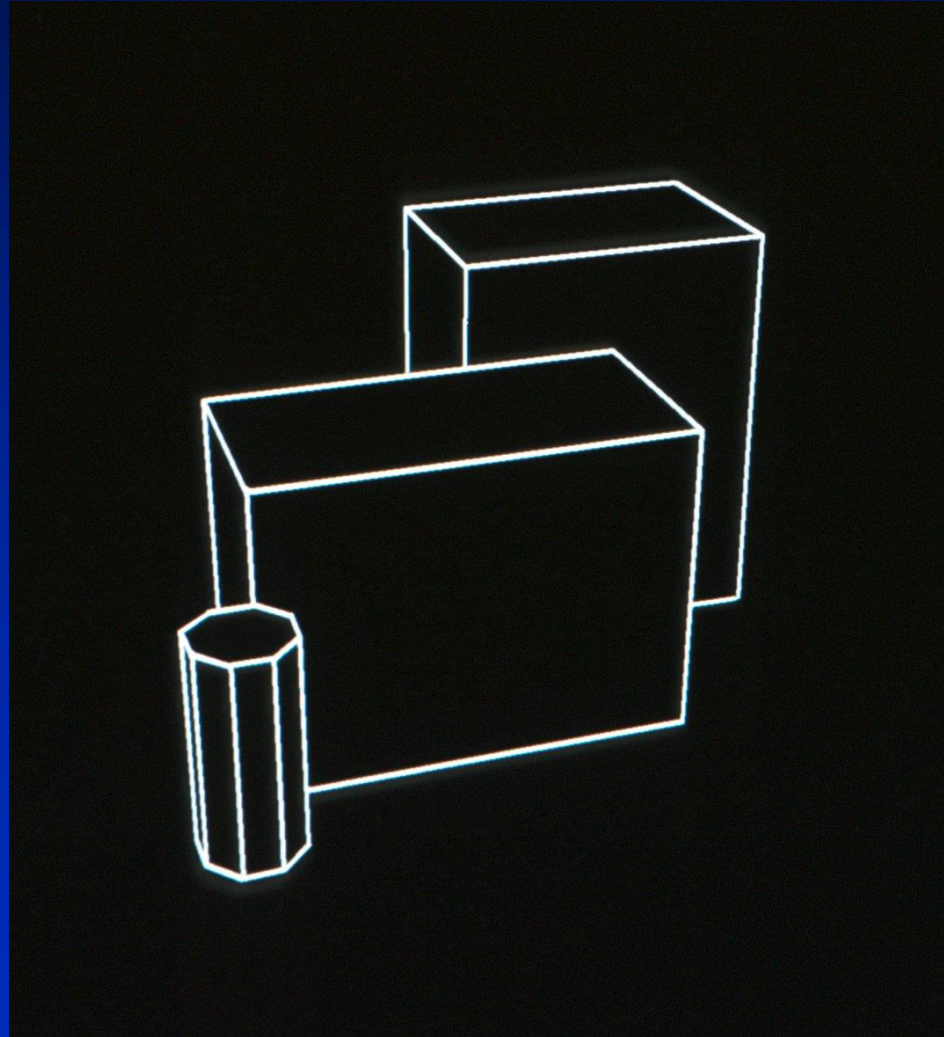
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# Hidden Line Algorithm

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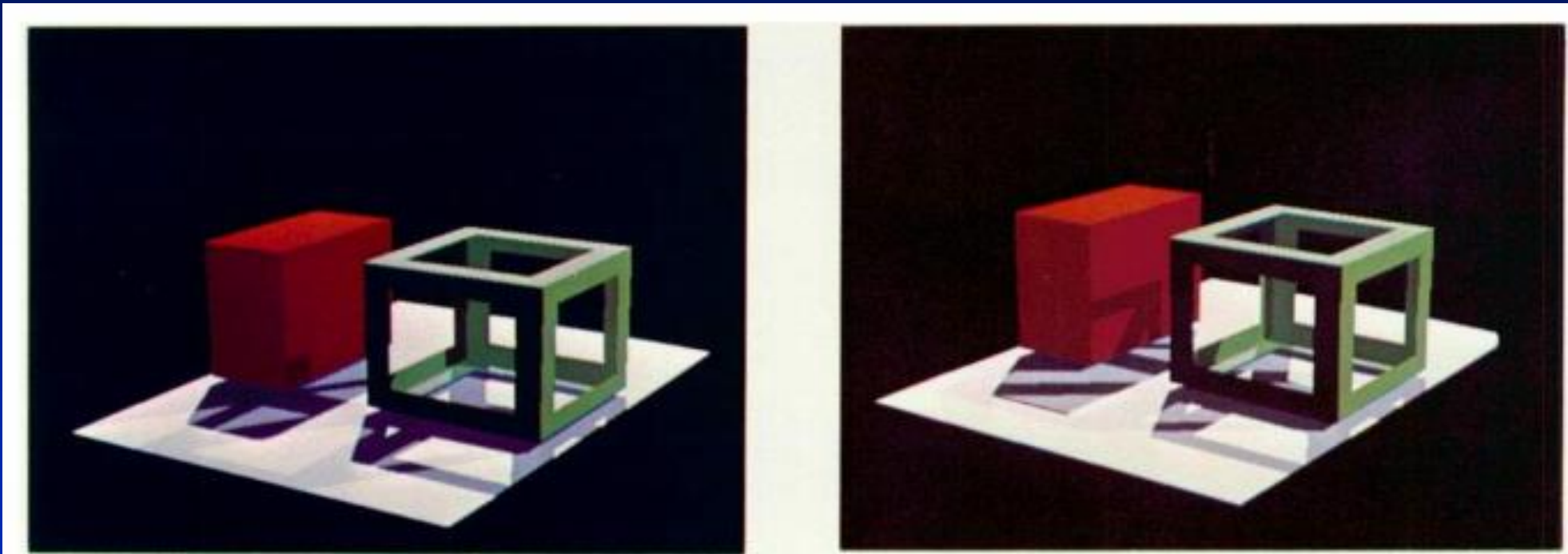
# E & S Frame Buffer

1975



\$80,000

# Weiler Atherton Shadow Algorithm



Figures 6. Shadowed Image Displays with Two Light Sources at Different Locations.

# Assumptions and Transformations

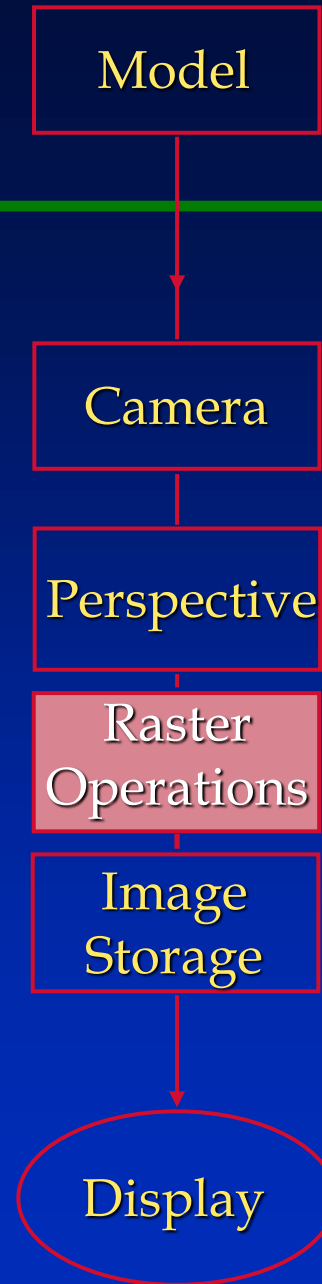
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- Lines into lines
- Planes into planes
- True perspective image
- Transformations preserves depth order

# Raster Operations

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- Conversion from polygons to pixels
- Hidden surface removal (z-buffer)
- Incremental shading



# Visible Surface Algorithm

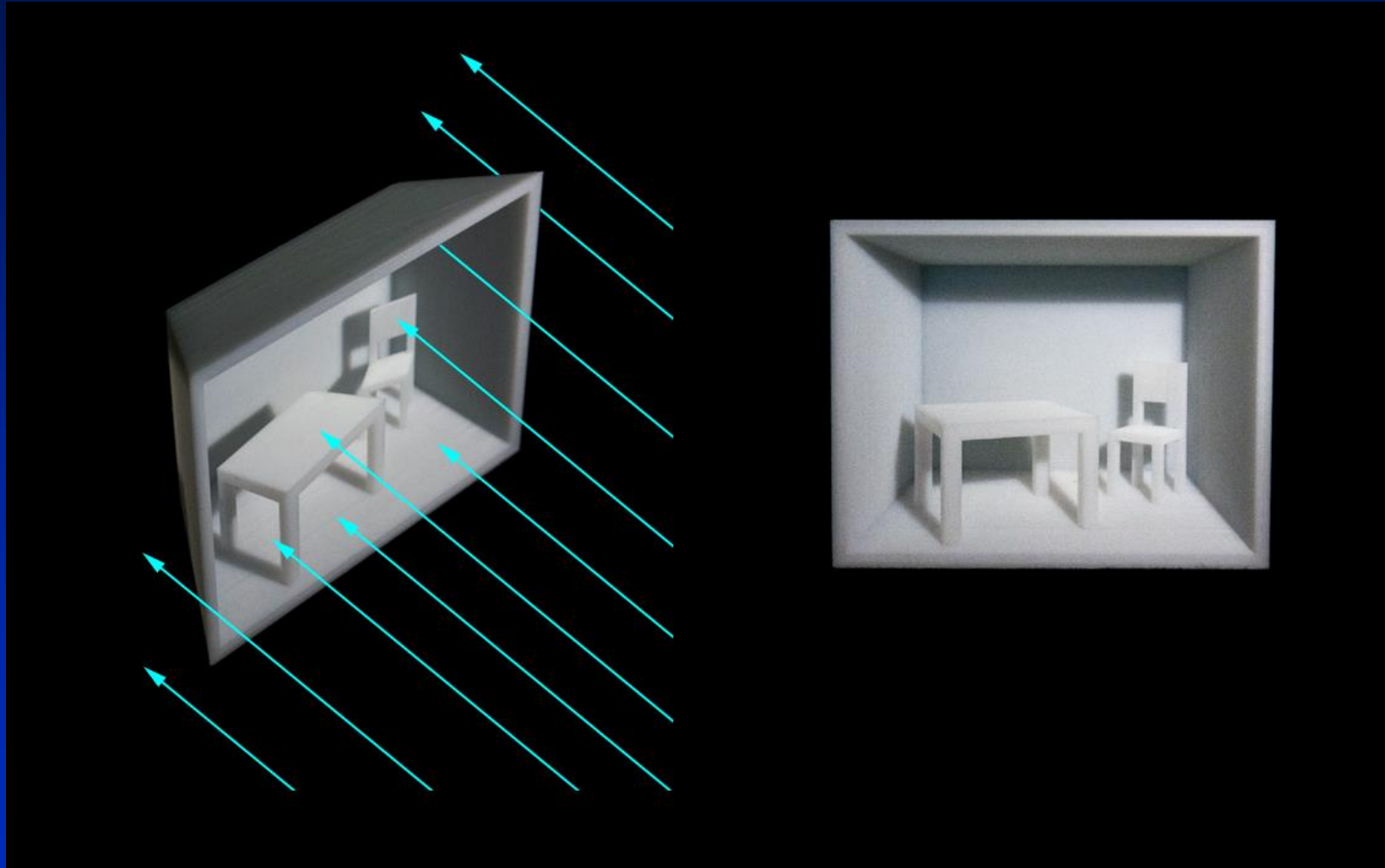
## Z-Buffer Algorithm

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1. Set  $\text{depth}(x, y) = 1.0$   
 $\text{intensity}(x, y) = \text{background color}$
2. For each polygon, find all pixels covered
3. Calculate  $z(x, y)$  of each pixel covered by the polygon

# Z-buffer

The distorted model in virtual image space is viewed from negative infinity and all rays are parallel to the view direction. (along the positive Z-axis)



The perspective image is identical.



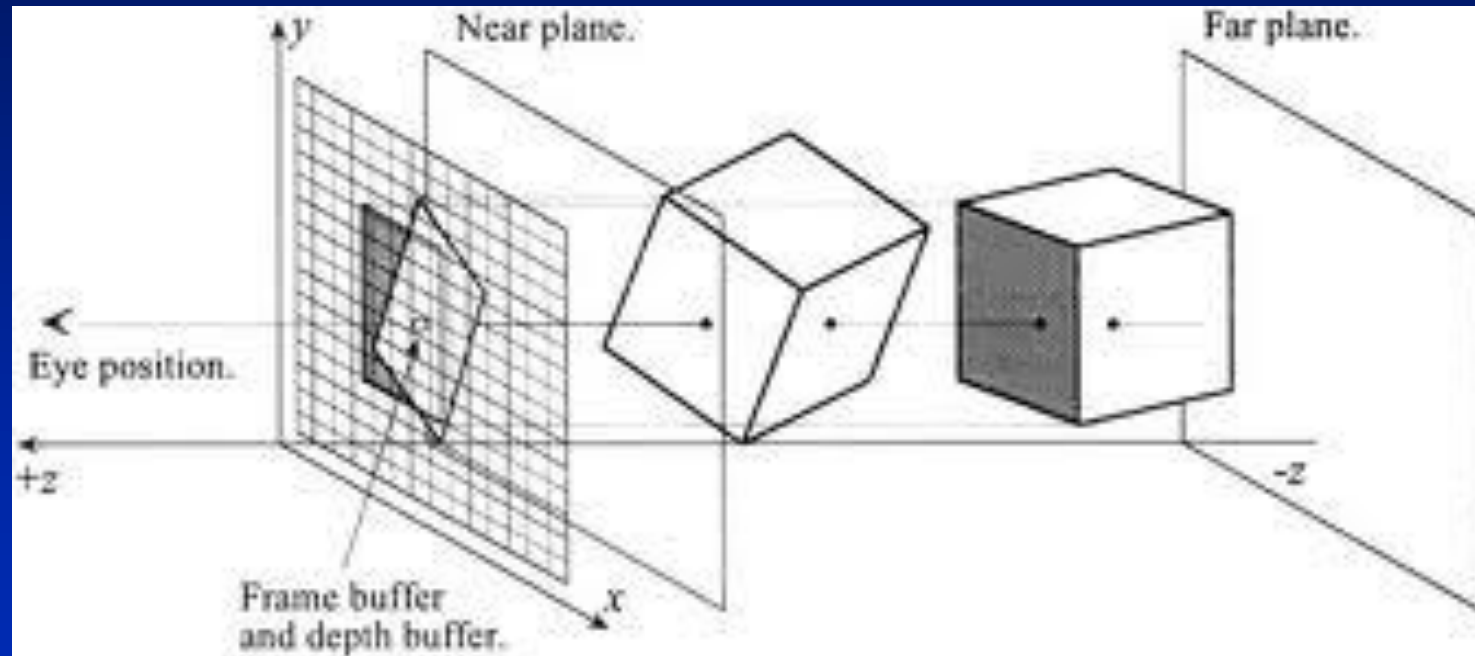
# Visible Surface Algorithm

## Z-Buffer Algorithm

---

1. Set  $\text{depth}(x, y) = 1.0$   
     $\text{intensity}(x, y) = \text{background color}$
2. For each polygon, find all pixels covered
3. Calculate  $z(x, y)$  of each pixel covered by the polygon
4. If  $z(x, y) < \text{depth}(x, y)$ , polygon is closer  
    set  $\text{depth}(x, y) = z(x, y)$   
    change color

# Depth Buffer Algorithm



# Image Storage

- Typical frame buffer
  - 1280 x 1024 pixels
  - 3 channels (red, green, blue)
  - 1 byte/channel
- Total memory
  - 3 3/4 megabytes - single buffer
  - 7 1/2 megabytes - double buffer



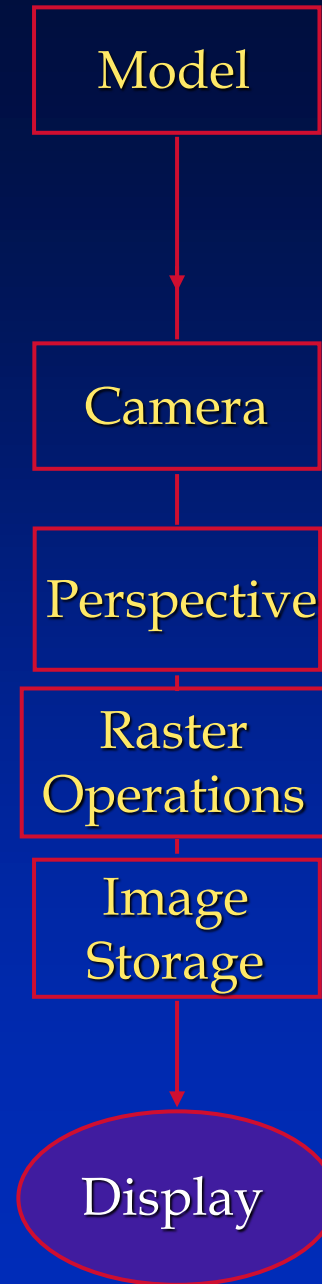
# Refresh vs. Update Rate

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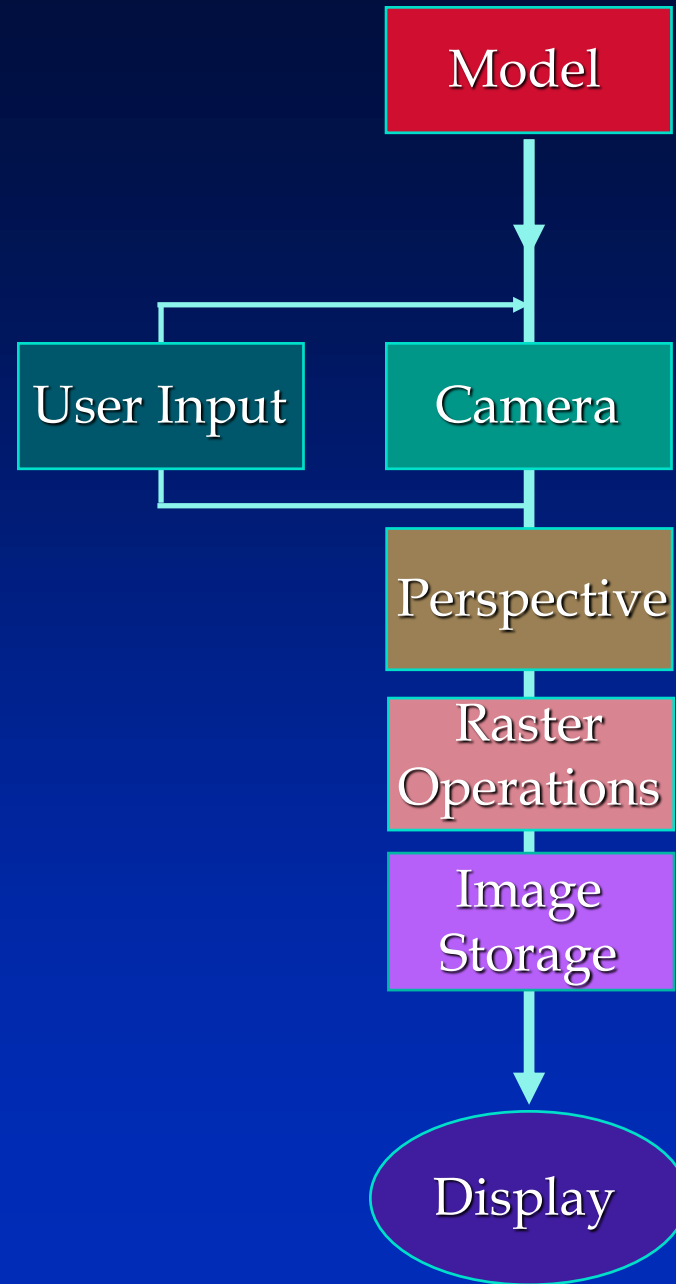
- The “refresh rate” is the number of times per second the entire image is drawn
- The “update rate” is the number of times per second the image is changed

# Display

- Digital to analog conversion
  - 1920 x 1080 resolution
  - 60 frames per second
- Total data rate
  - 2 million pixels
  - x 3 bytes/pixel
  - x 60 frames/second
  - = 360 megabytes/second



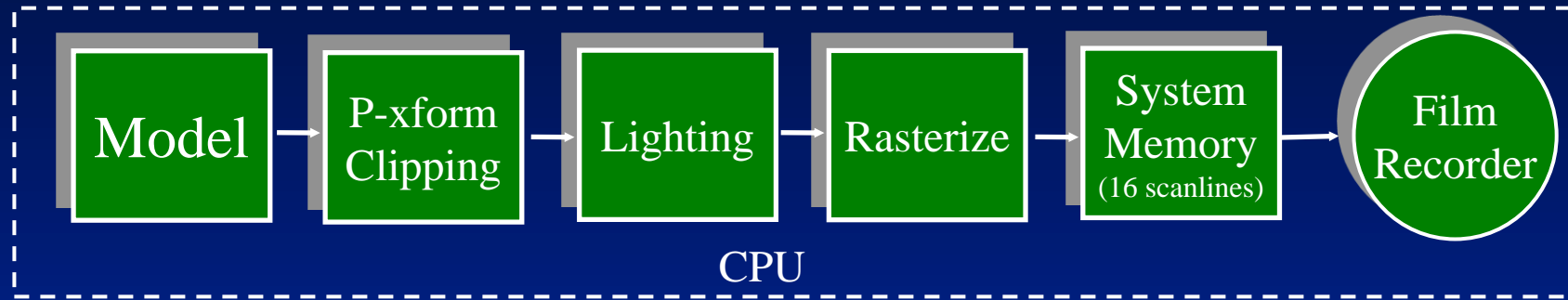
# Direct Illumination



# Graphics Hardware Pipeline

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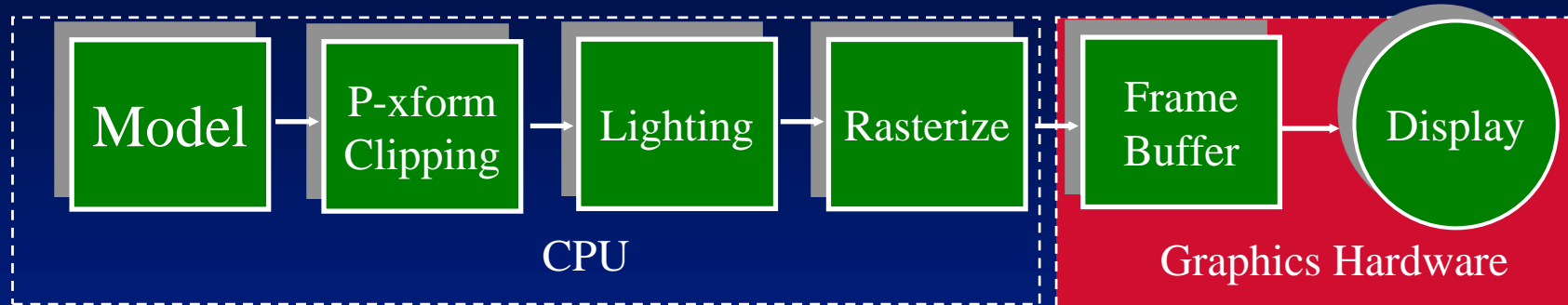
# Graphics Hardware circa 1970



- System used to generate Phong goblet



# Graphics Hardware circa 1975

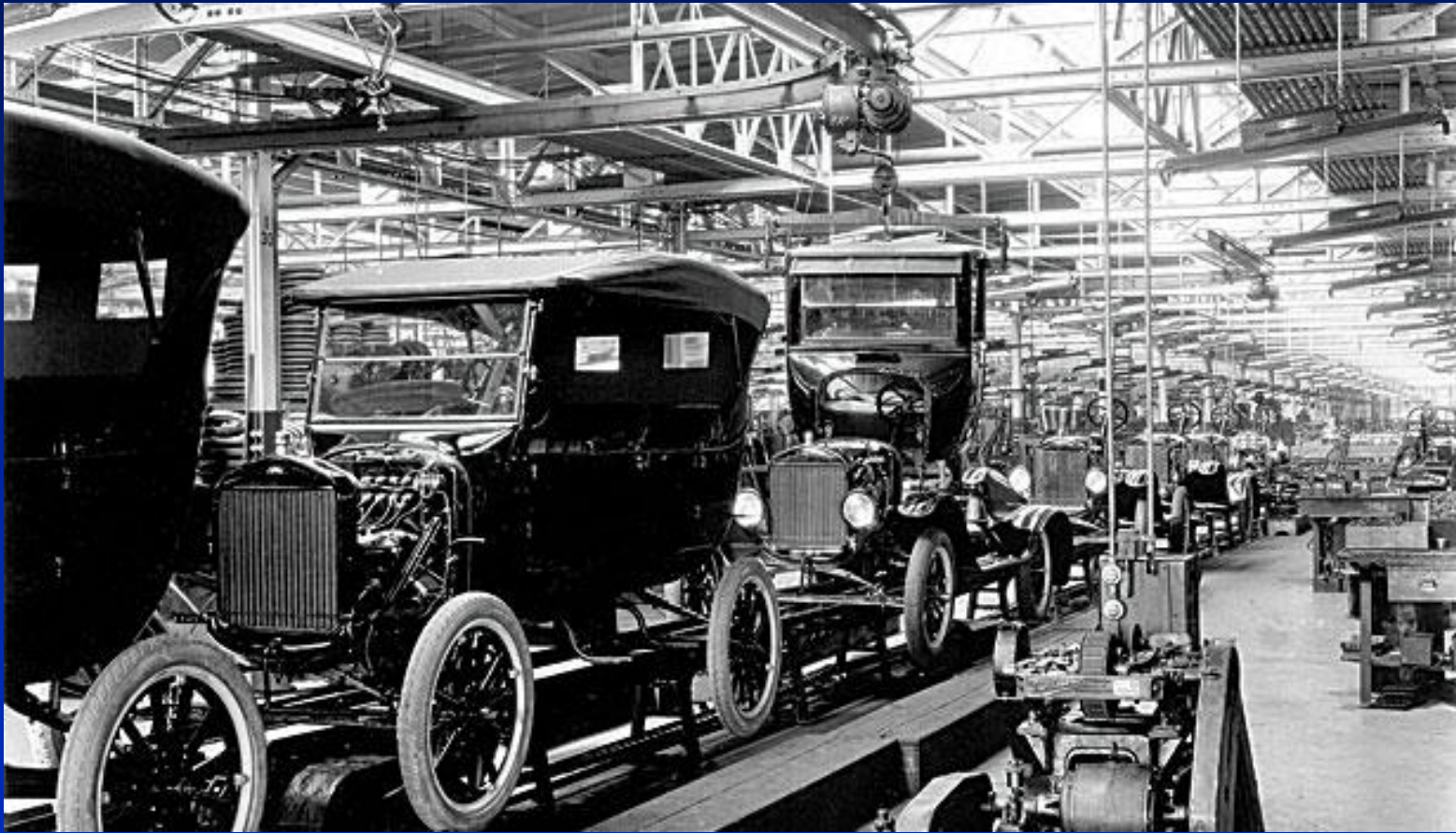


## Cost of Memory Prohibitive

- 512x480x8 bit frame buffer cost \$80,000!
- No z-buffer (at 24 or 32 bits/pixel, it requires even more memory than FB)
- Only single frame buffer
- all work done in CPU until frame buffer(slow!)

# Ford's Pipeline

1913



# Why a Pipeline?

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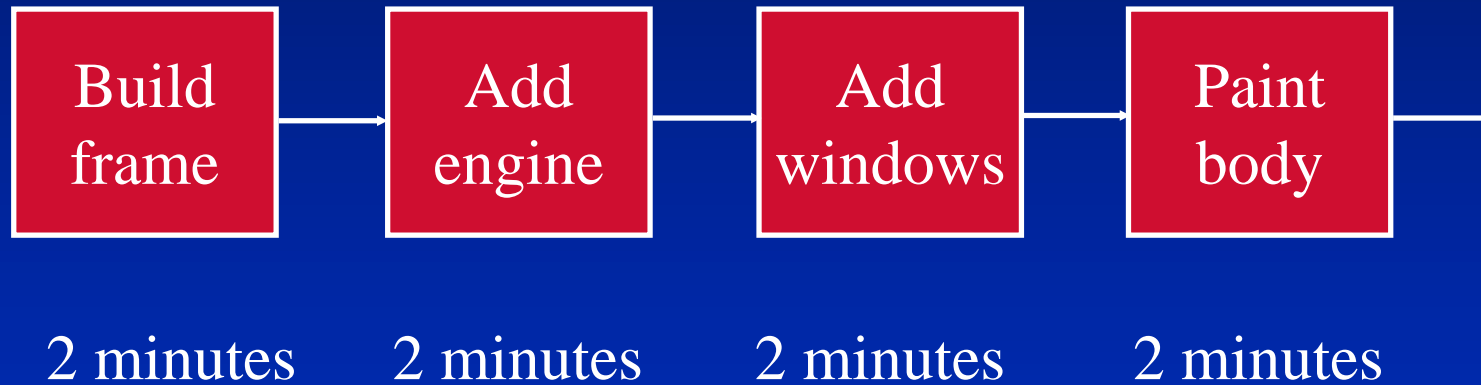
A pipeline allows multiple processes to occur in parallel. Example:

- An automobile assembly line. Assume 4 stations, each taking 2 minutes to do its task. It takes 8 minutes to make a car, but the *rate* at which cars are made is one every 2 minutes.

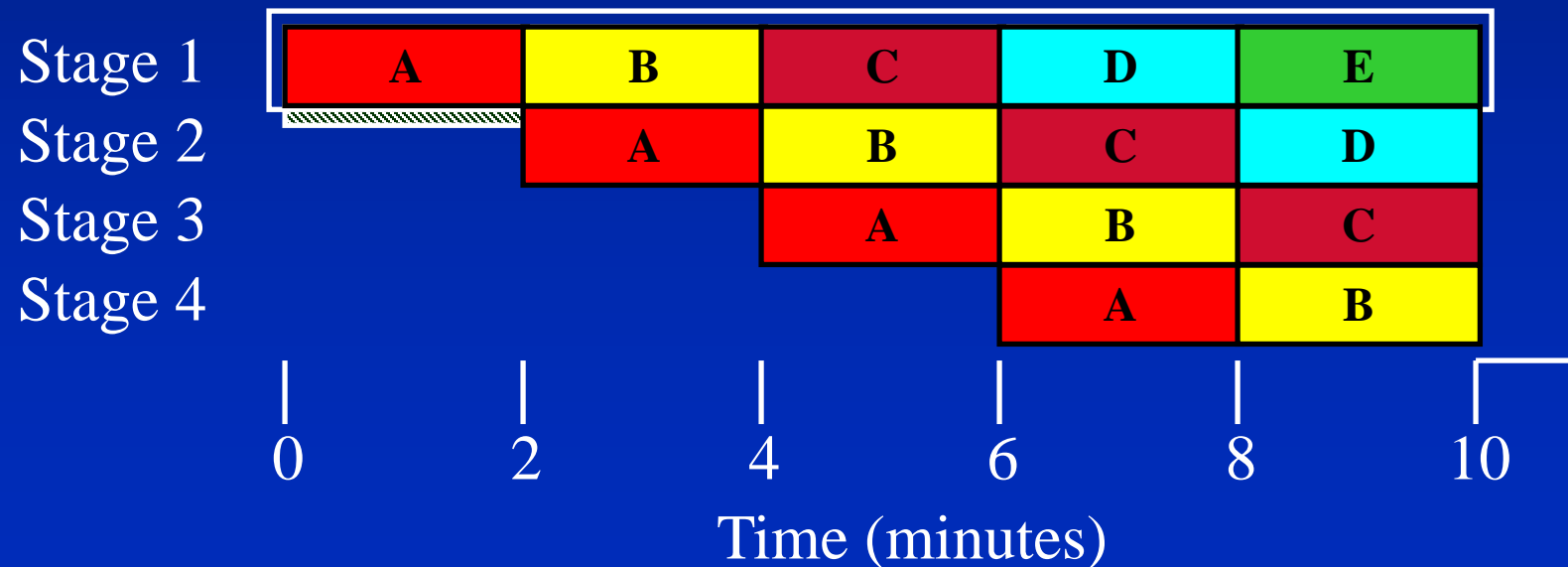
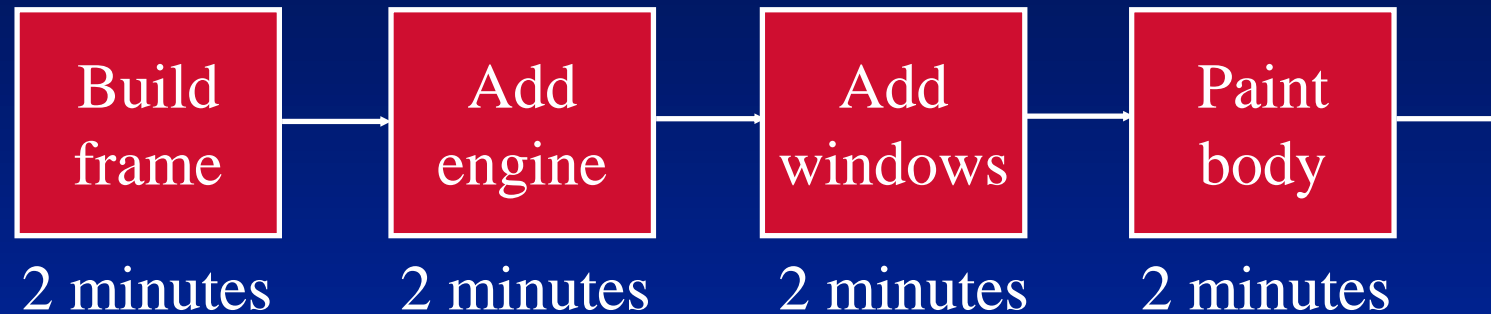
# Example: Automobile Pipeline

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Automobile takes 8 minutes to make, but the assembly line makes a car every two minutes.



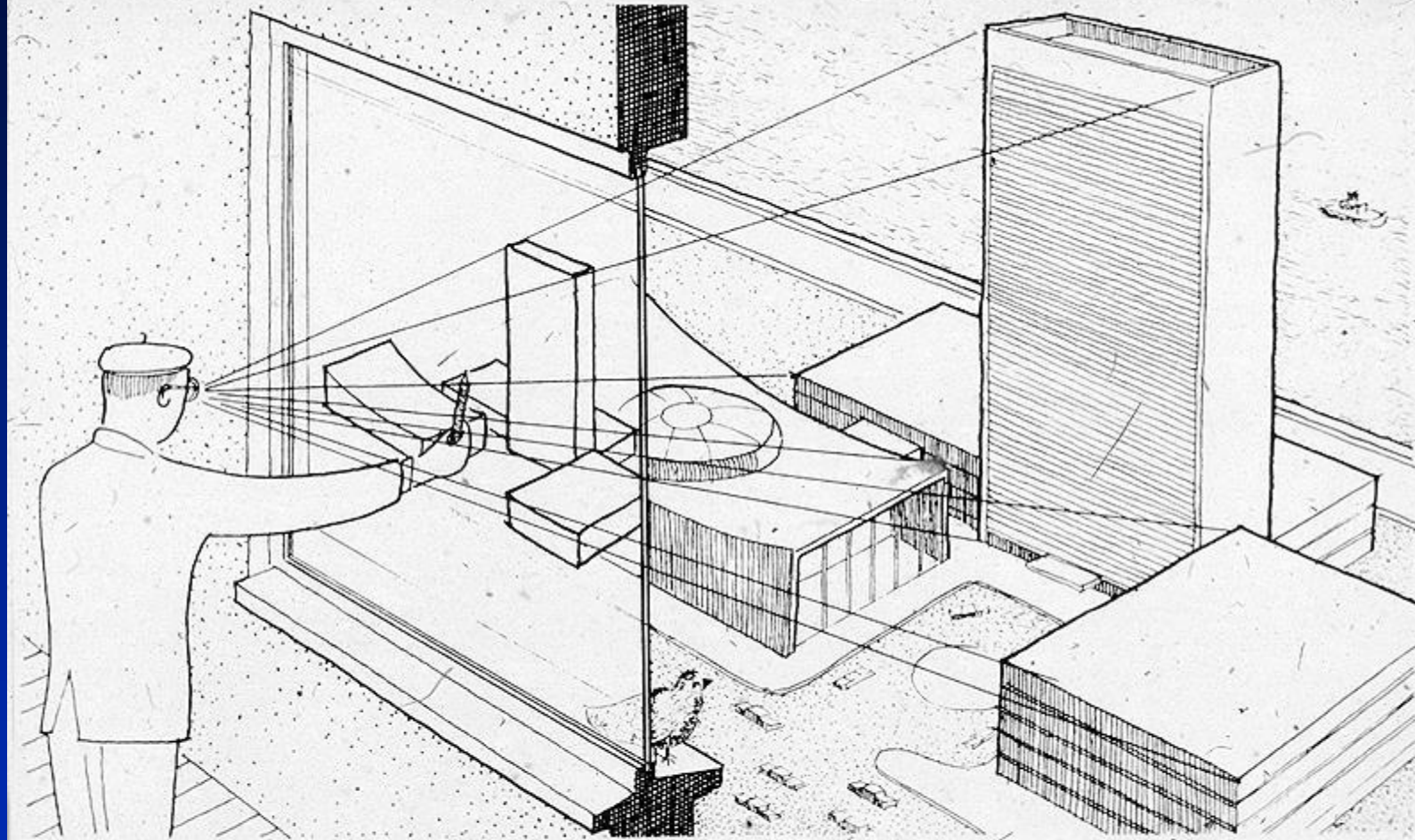
Automobile takes 8 minutes to make, but the assembly line makes a car every two minutes.



# 1984 - Clark's Geometry Engine

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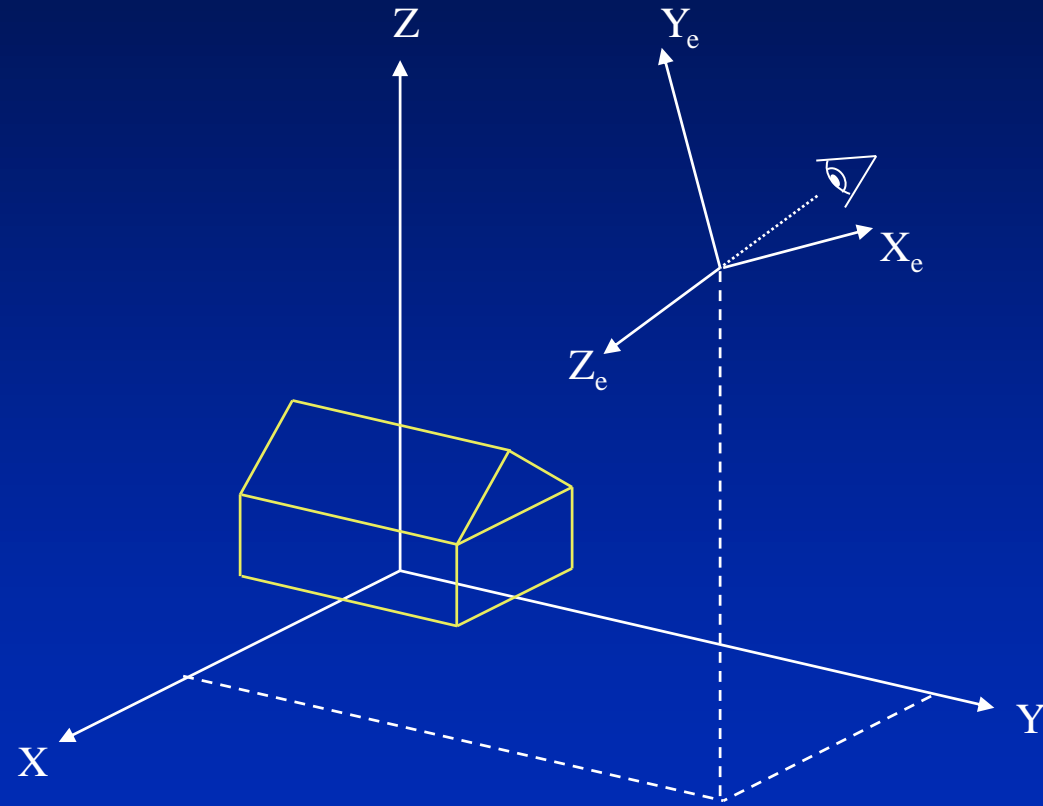
- Special Purpose four component vector floating point processor
- Same chip is software re-configurable to perform the three basic operations in computer graphics
  - matrix transformations
  - clipping
  - mapping to output device coordinates



The concept of the picture plane may be better understood by looking through a window or other transparent plane from a fixed viewpoint. Your lines of sight, the multitude of straight lines leading from your eye to the subject, will all intersect this plane. Therefore, if you were to reach out with a grease pencil and draw the image of the subject on this plane you would be "tracing out" the infinite number of points of intersection of sight rays and plane. The result would be that you would have "transferred" a real three-dimensional object to a two-dimensional plane.

# Eye Coordinate System

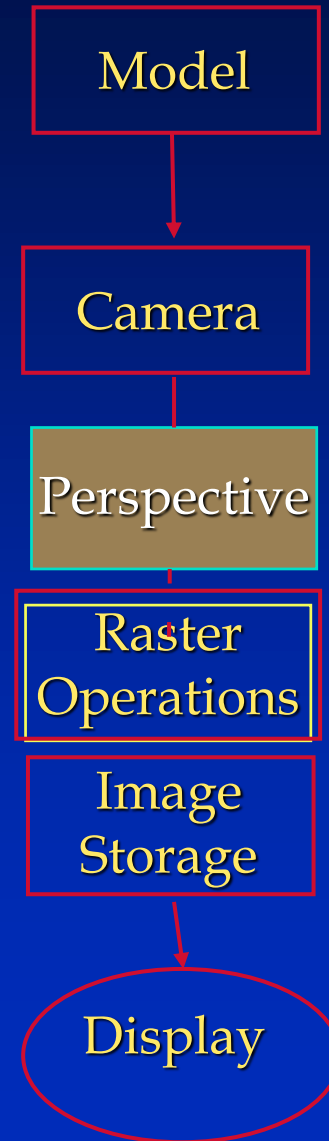
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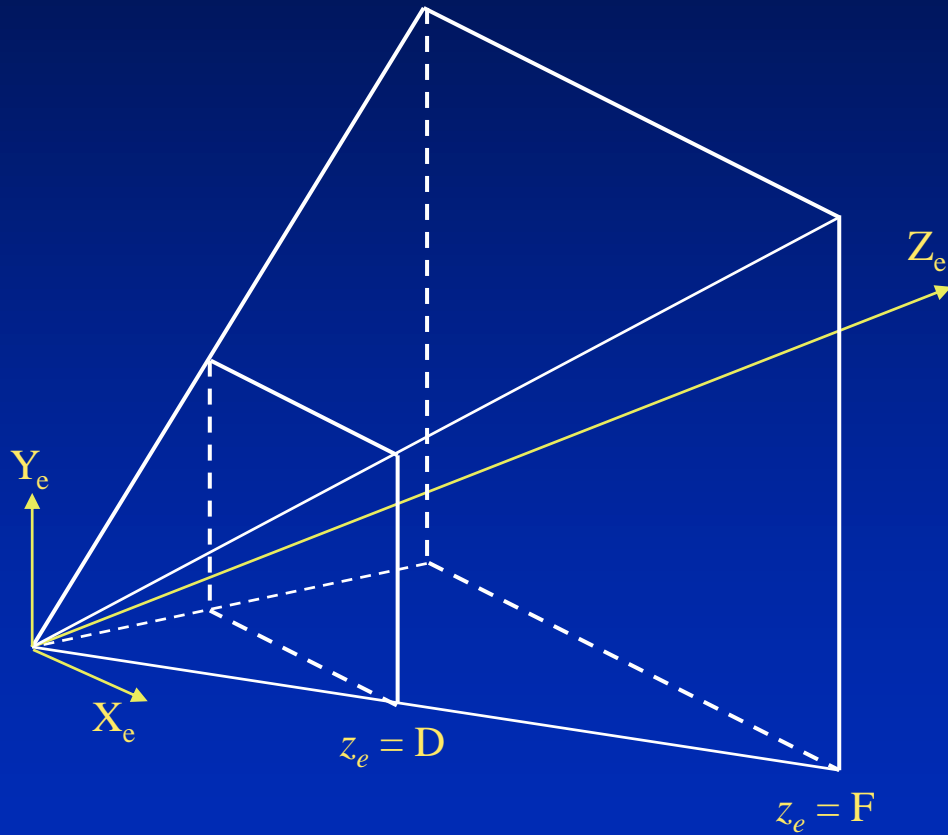


# Perspective Transformation

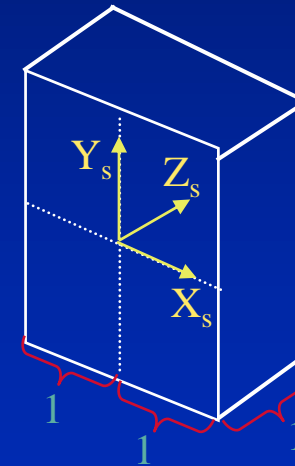
- Perspective transformation  
4 (4x4) Matrix multiplications



# Clipping to a Viewing Frustum



Frustum of vision



Screen coordinate system

# Clipping to a Viewing Frustum

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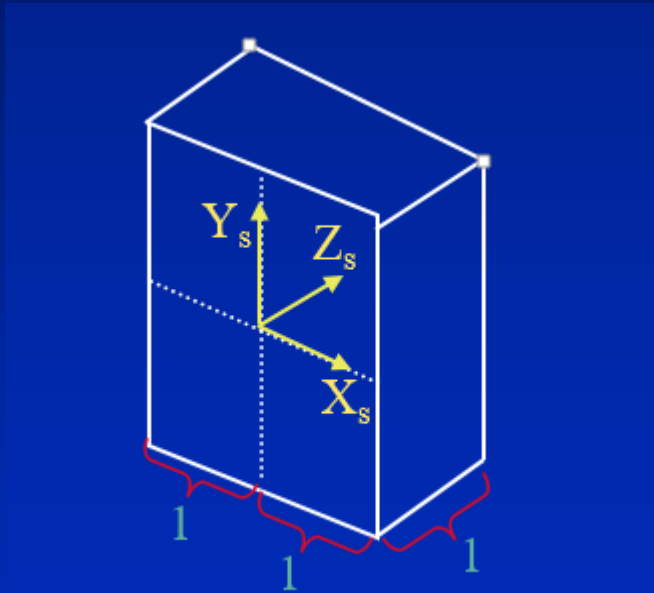
- Perspective transformation
  - 4 (4x4) Matrix multiplications
- Clipping
  - 6 (4x4) Matrix multiplications

# Viewport Mapping

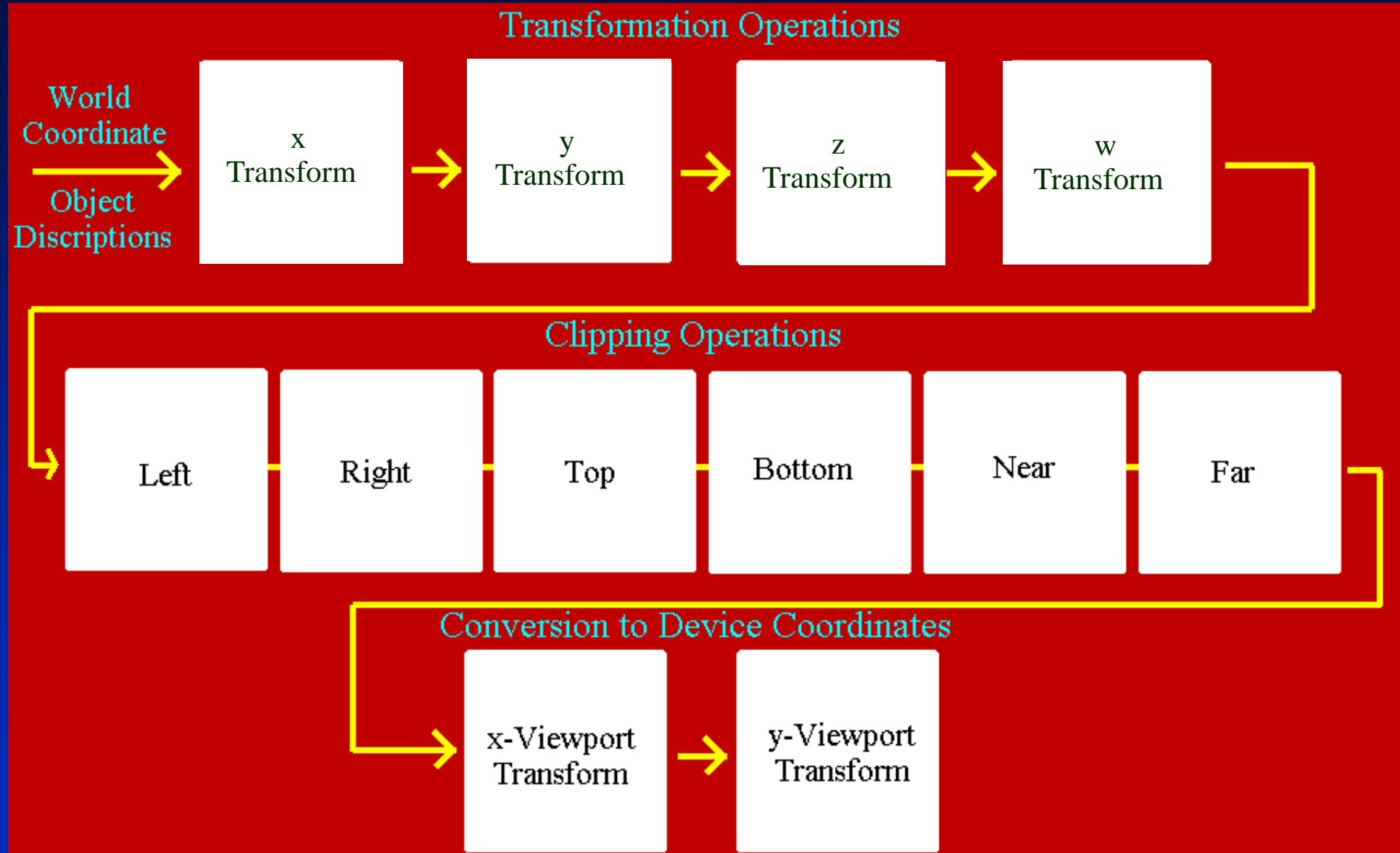
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- Perspective transformation
  - 4 (4x4) Matrix multiplications
- Clipping
  - 6 (4x4) Matrix multiplications
- Viewport mapping
  - 2 (4x4) Matrix multiplications

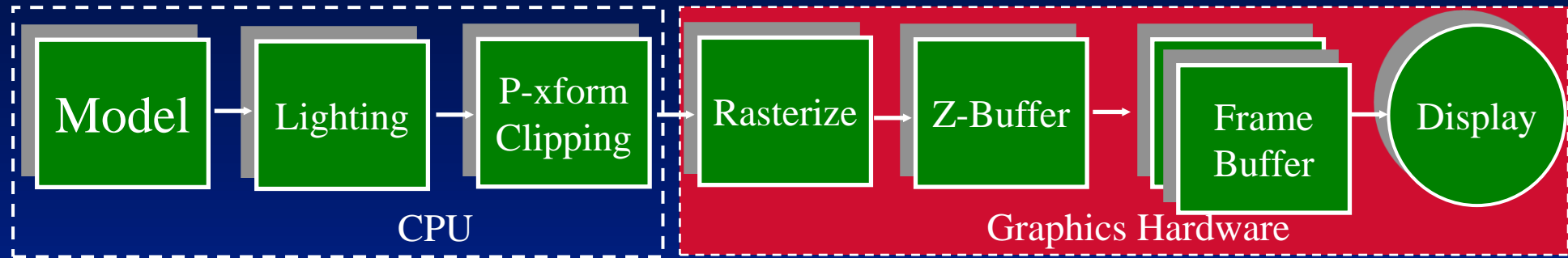
# Viewport Mapping



# 1984 - Clark's Geometry Engine

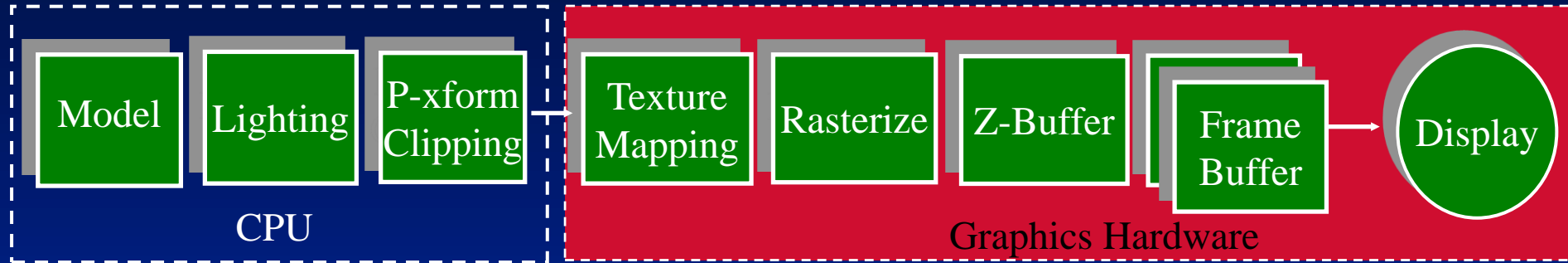


# Graphics Hardware circa 1986



- Added Z-Buffer
- Added Double Frame Buffer
- Rasterization performed in hardware

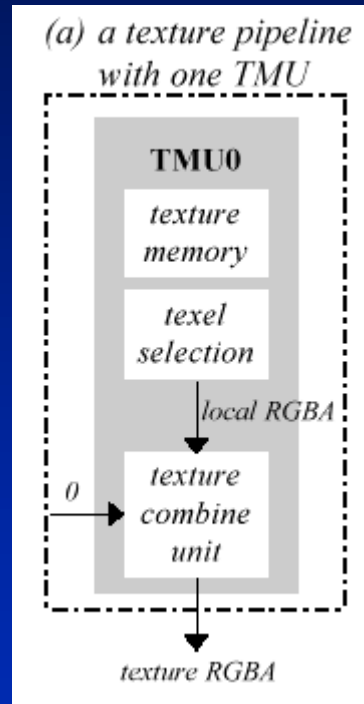
# Graphics Hardware 1999



- Addition of texture mapping units
- With texturing, high resolution detail is possible with relatively simple geometry



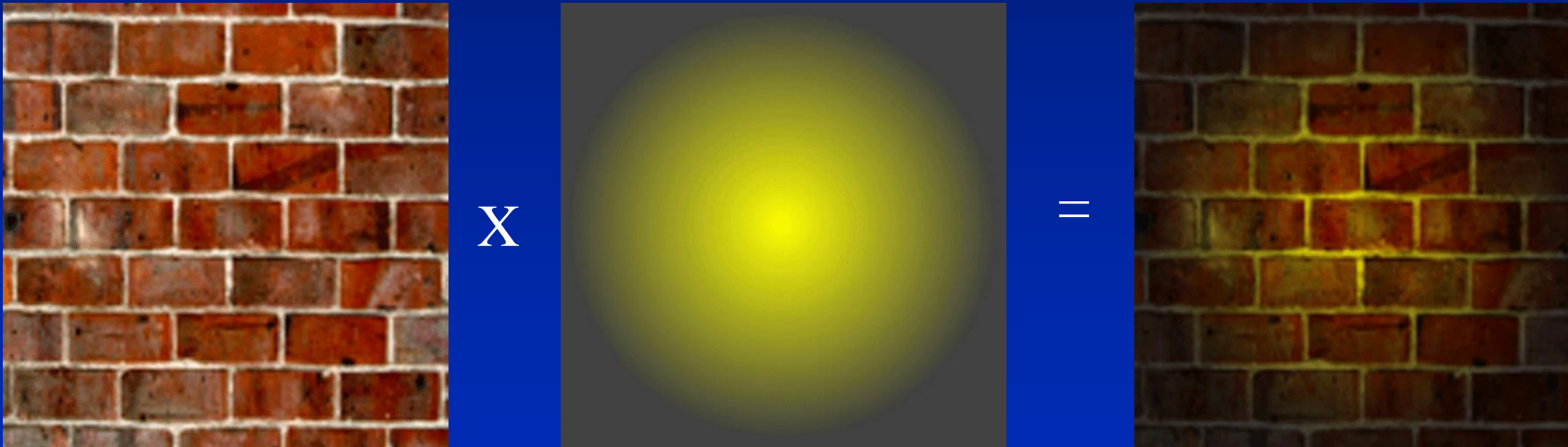
# Texture Mapping Units - TMU's



- A system with one TMU extracts the appropriate texel or texels from texture memory, minifies or magnifies it and filters it
- The texturecombine unit can scale the result

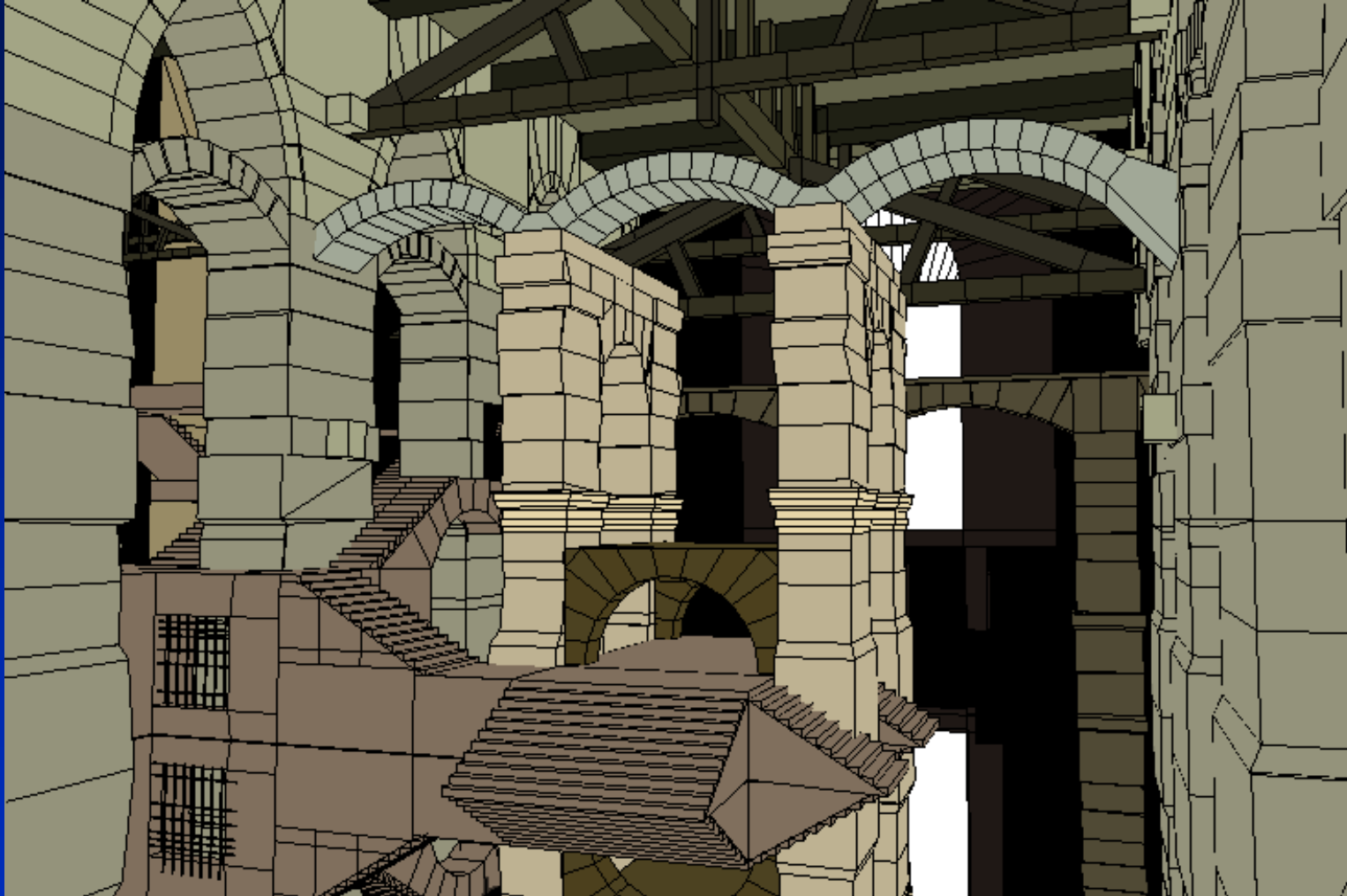
# Multipass Example: Light Maps

- Two separate textures, one for the material's composition, one for the lighting



*J.L.Mitchell, M. Tatro, and I. Bullard*

# Castle's Geometry



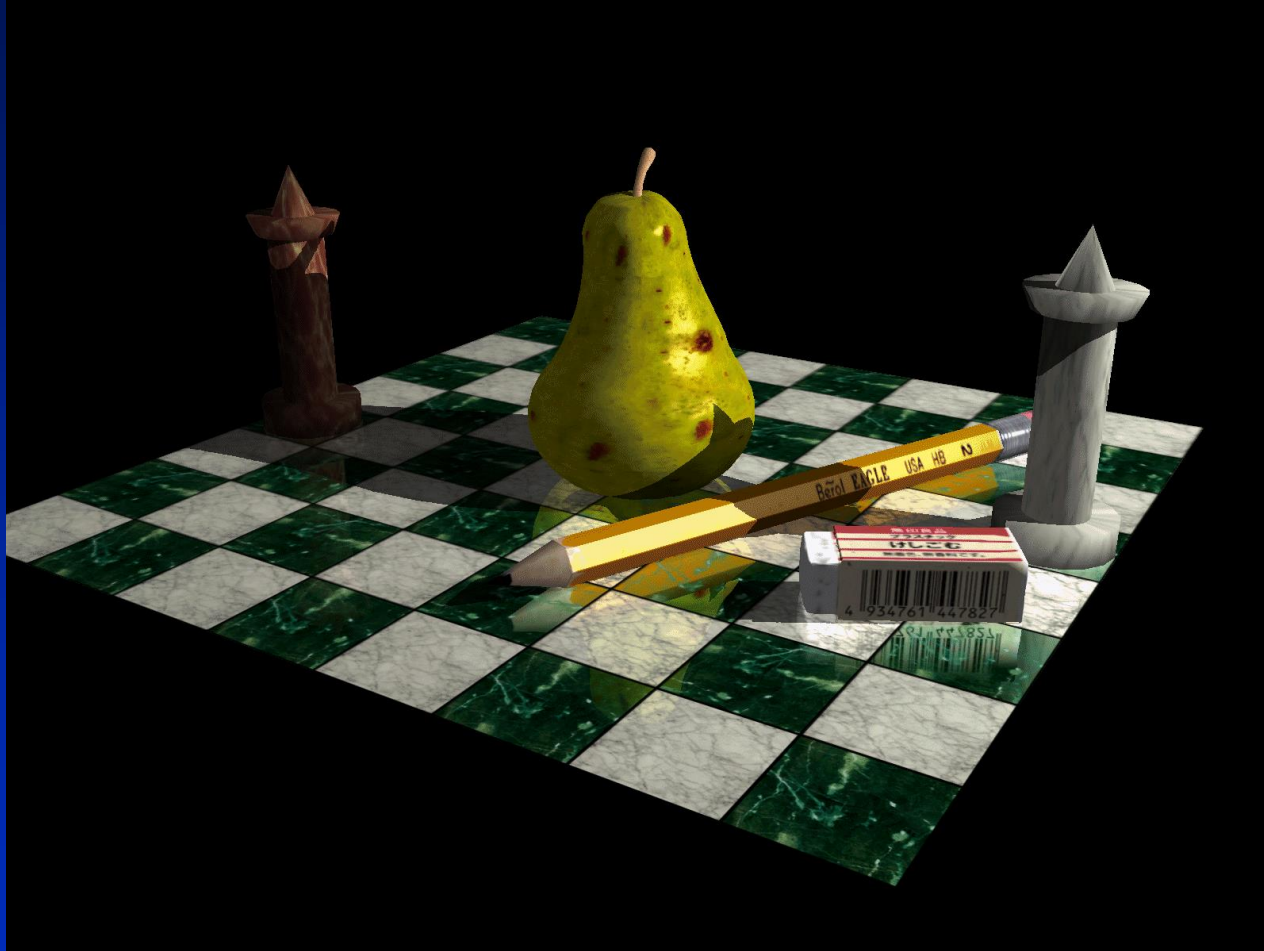
*Agata & Andrzej Wojaczek, Advanced Graphics Applications Inc.*

# Reflection Example - Castle



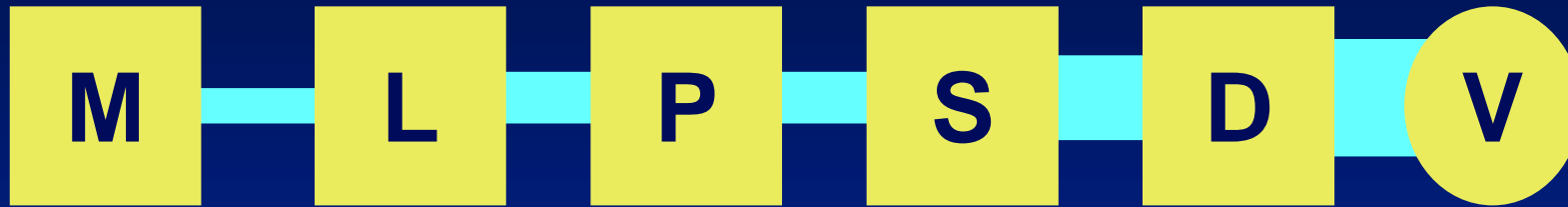
*Agata & Andrzej Wojaczek, Advanced Graphics Applications Inc.*

# Putting it all together



Gloss textures on pear, shadows on curved surfaces, reflections dropping off with depth from table.

# Graphics Pipeline - 1980's



**M — Model**

**L — Lighting**

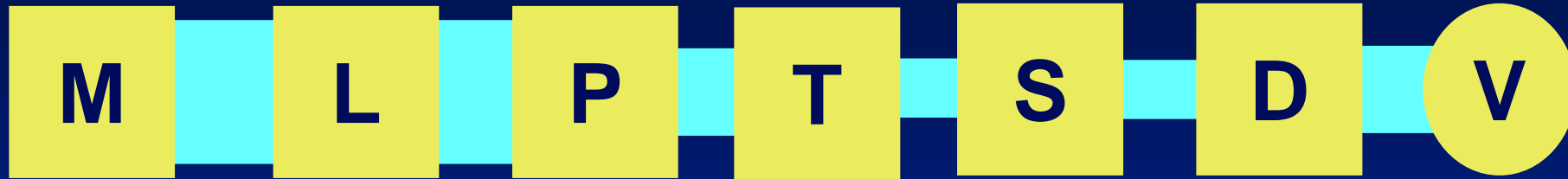
**P — Perspective/Clipping**

**S — Scan Conversion/Z-buffer**

**D — Display Storage**

**V — Video**

# Graphics Pipeline - 2000 +



**M — Model**

**L — Lighting**

**P — Perspective/Clipping**

**T — Texturing**

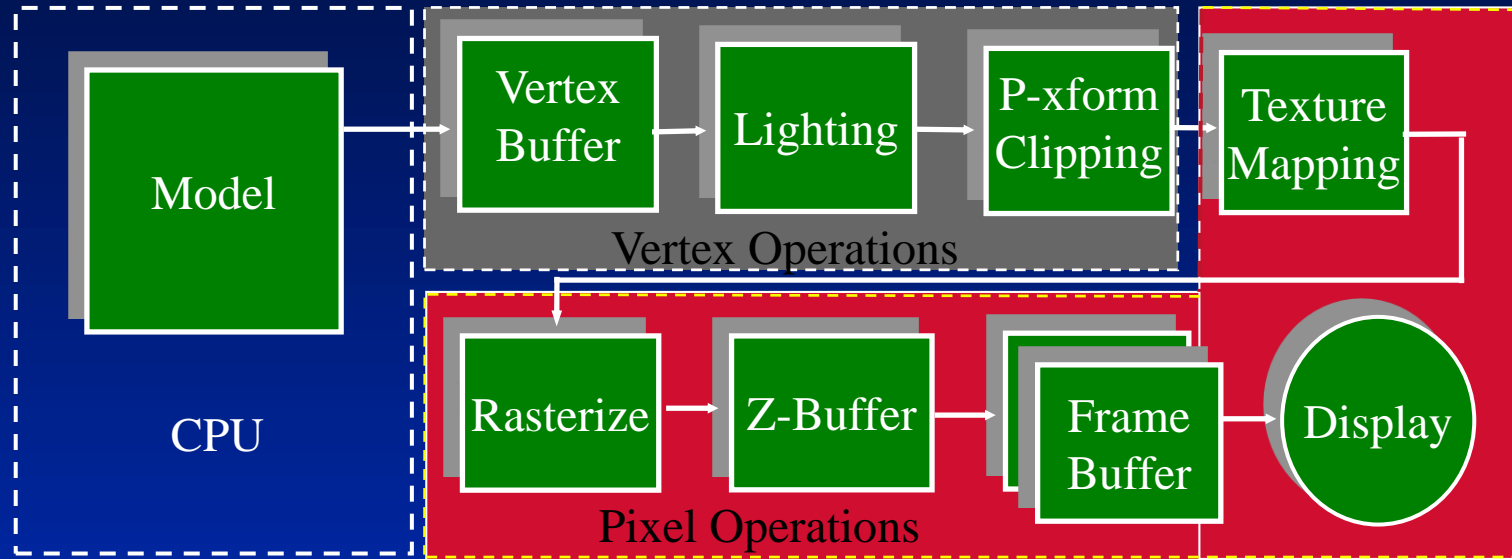
**S — Scan Conversion/Z-buffer**

**D — Display Storage**

**V — Video**

# Graphics Hardware

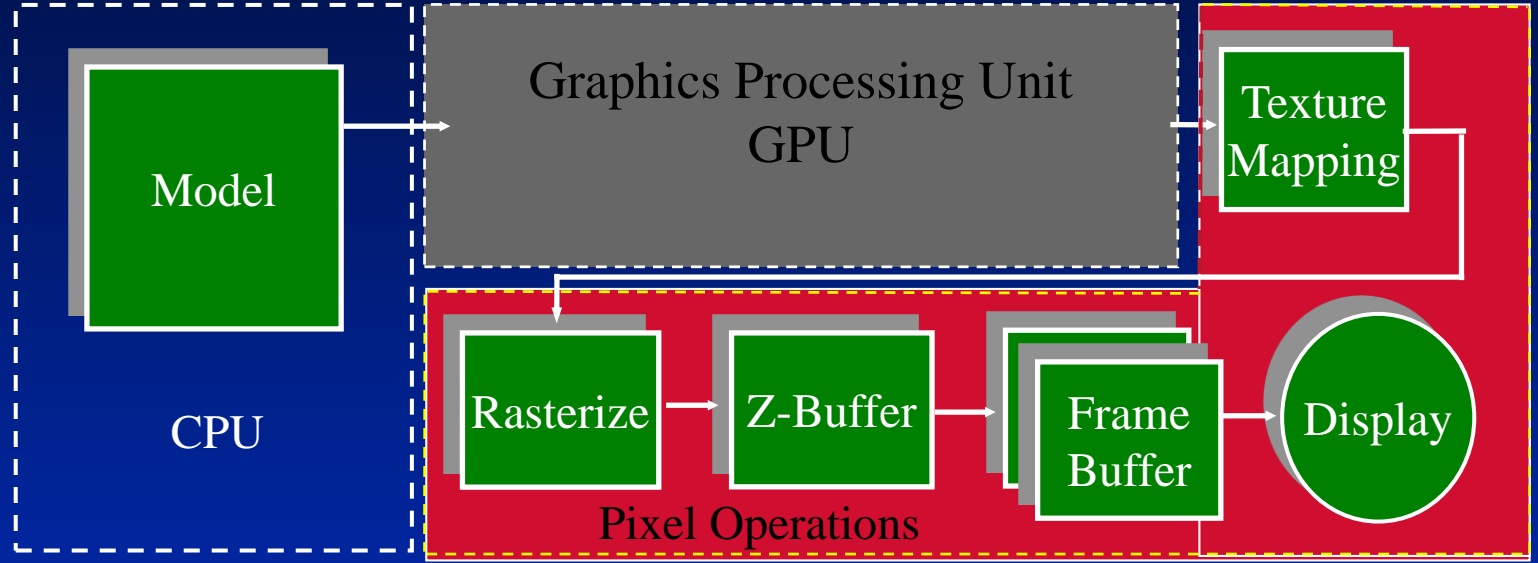
2003



- Early GPU's performed lighting and clipping operations on locally stored model



# Graphics Hardware 2003+



# Intel – Integrated Graphics

## 2013

“SANDY BRIDGE”



17%  
GPU\*



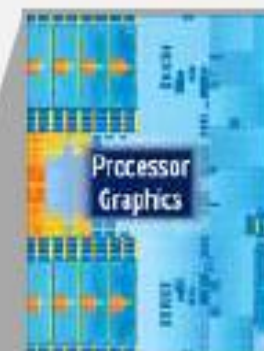
“IVY BRIDGE”



27%  
GPU\*



“HASWELL”  
Estimated



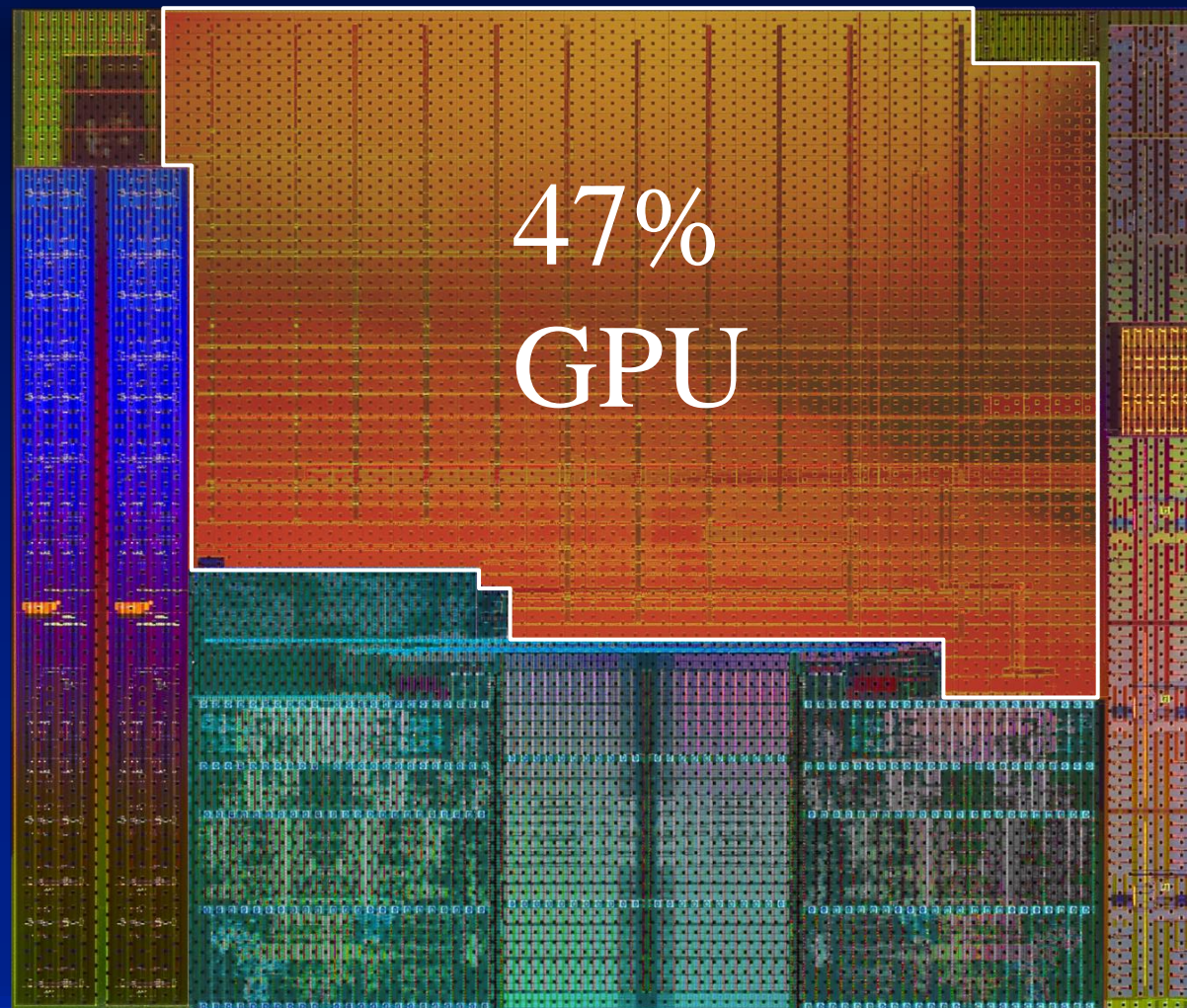
31%  
GPU\*



# AMD – Integrated Graphics

2014

- “Kaveri”
- 28 nm
- 47% GPU

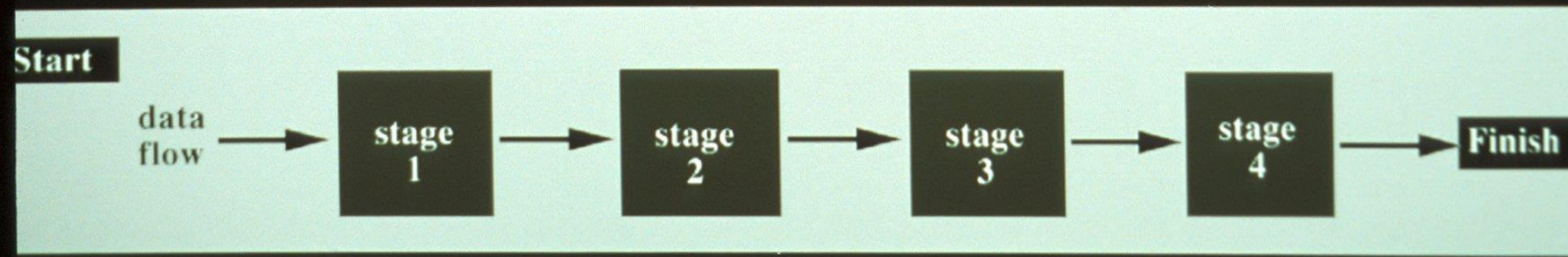
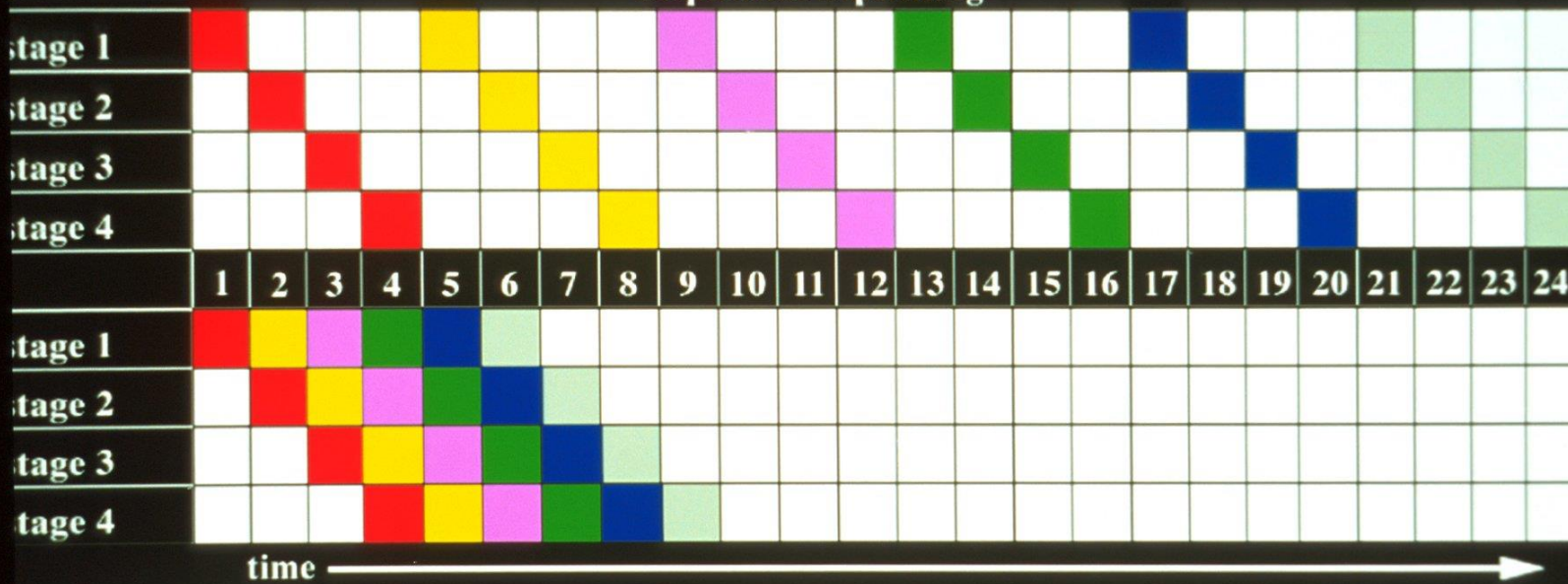


**End**

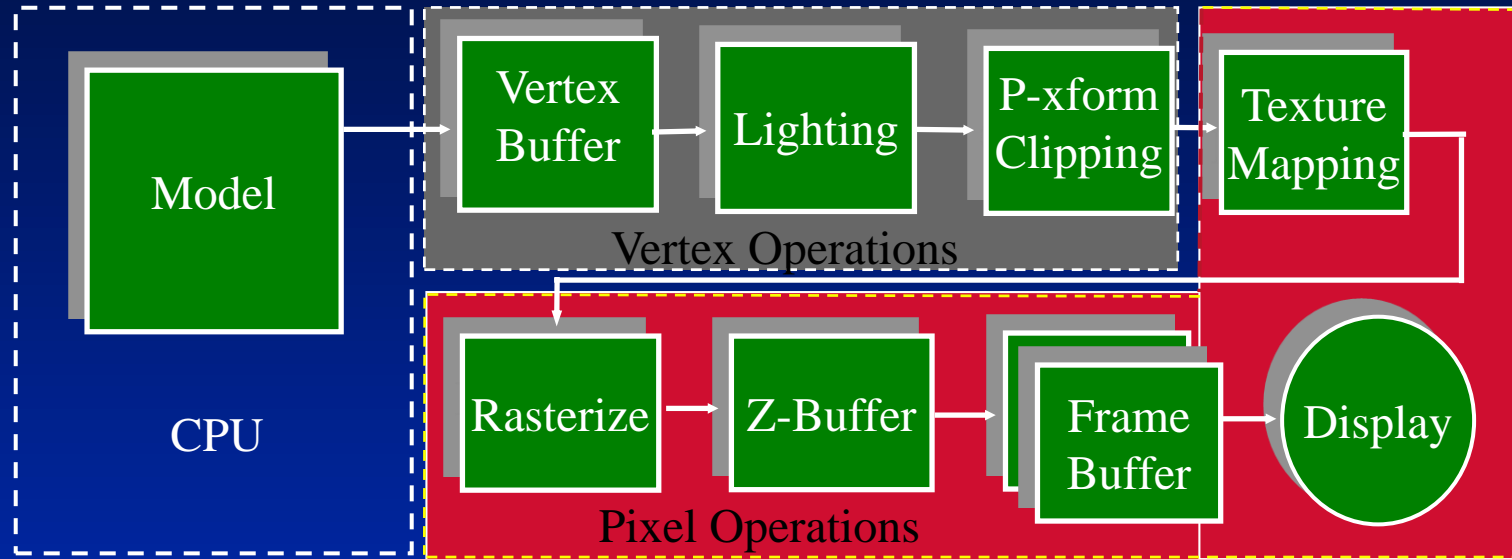
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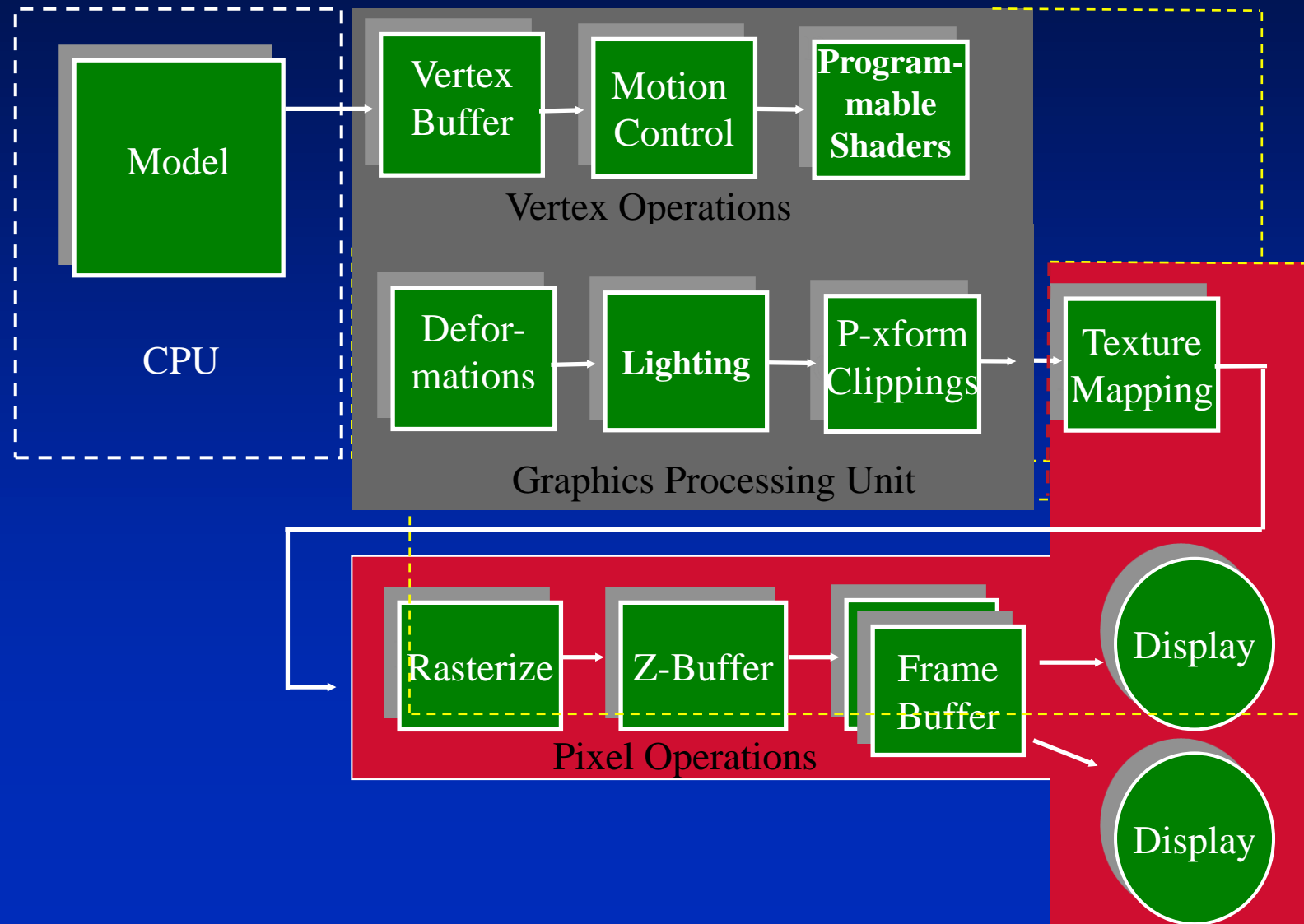
## Sequential Processing vs. Sequential Pipelining



# Graphics Hardware 2001

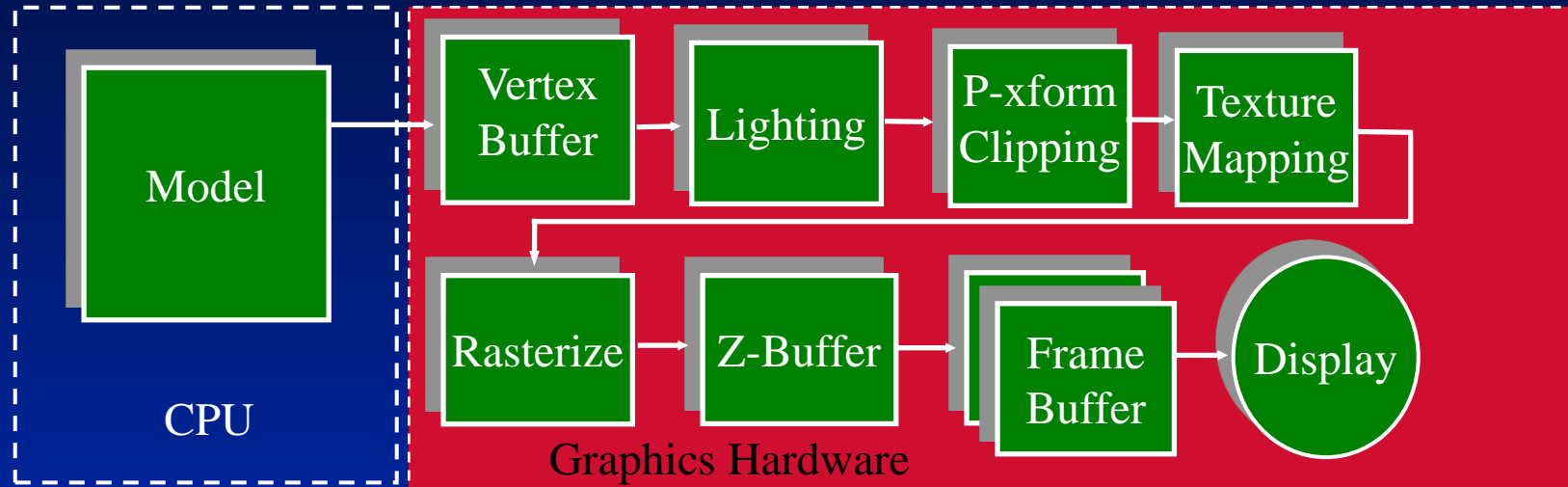


# Graphics Hardware 2005

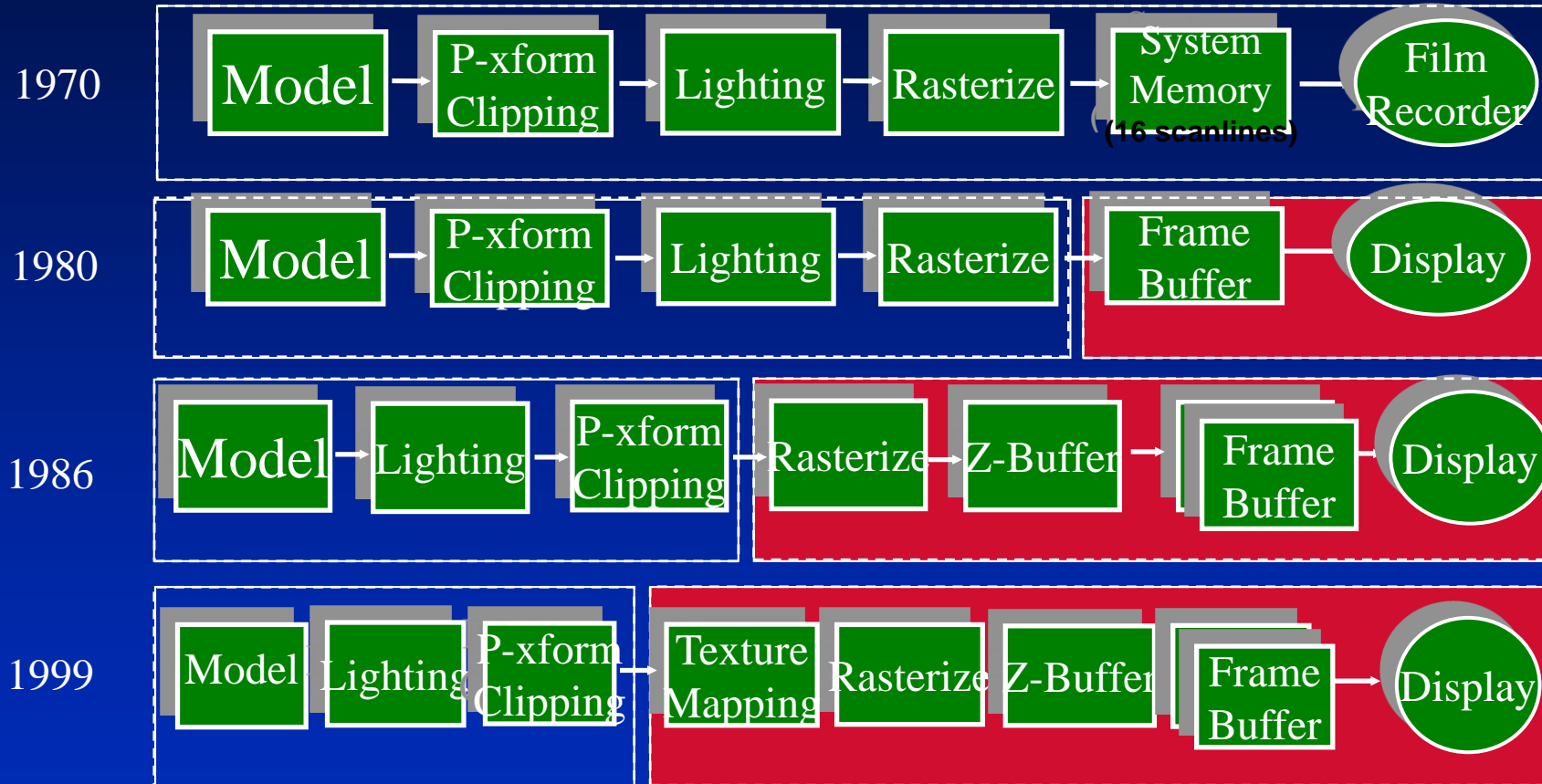




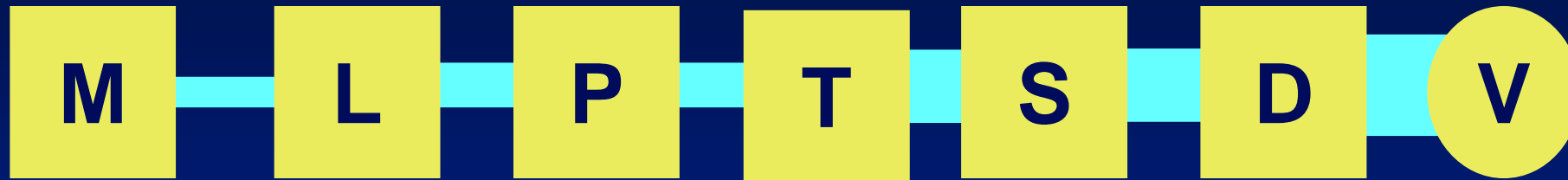
# Graphics Hardware 2000



# Graphics Hardware Recap



# Graphics Pipeline - 1990's



**M — Model**

**L — Lighting**

**P — Perspective/Clipping**

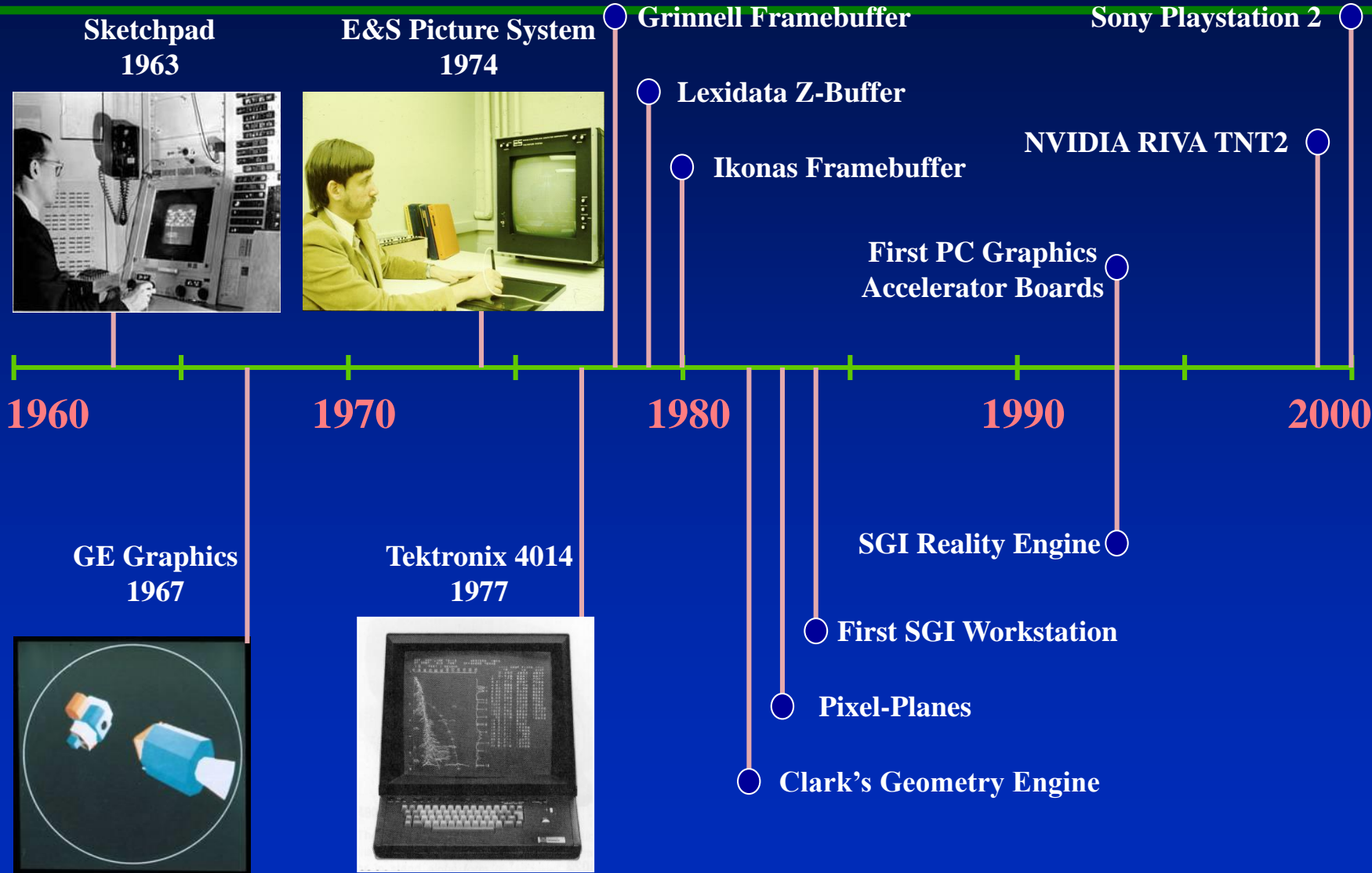
**T — Texturing**

**S — Scan Conversion/Z-buffer**

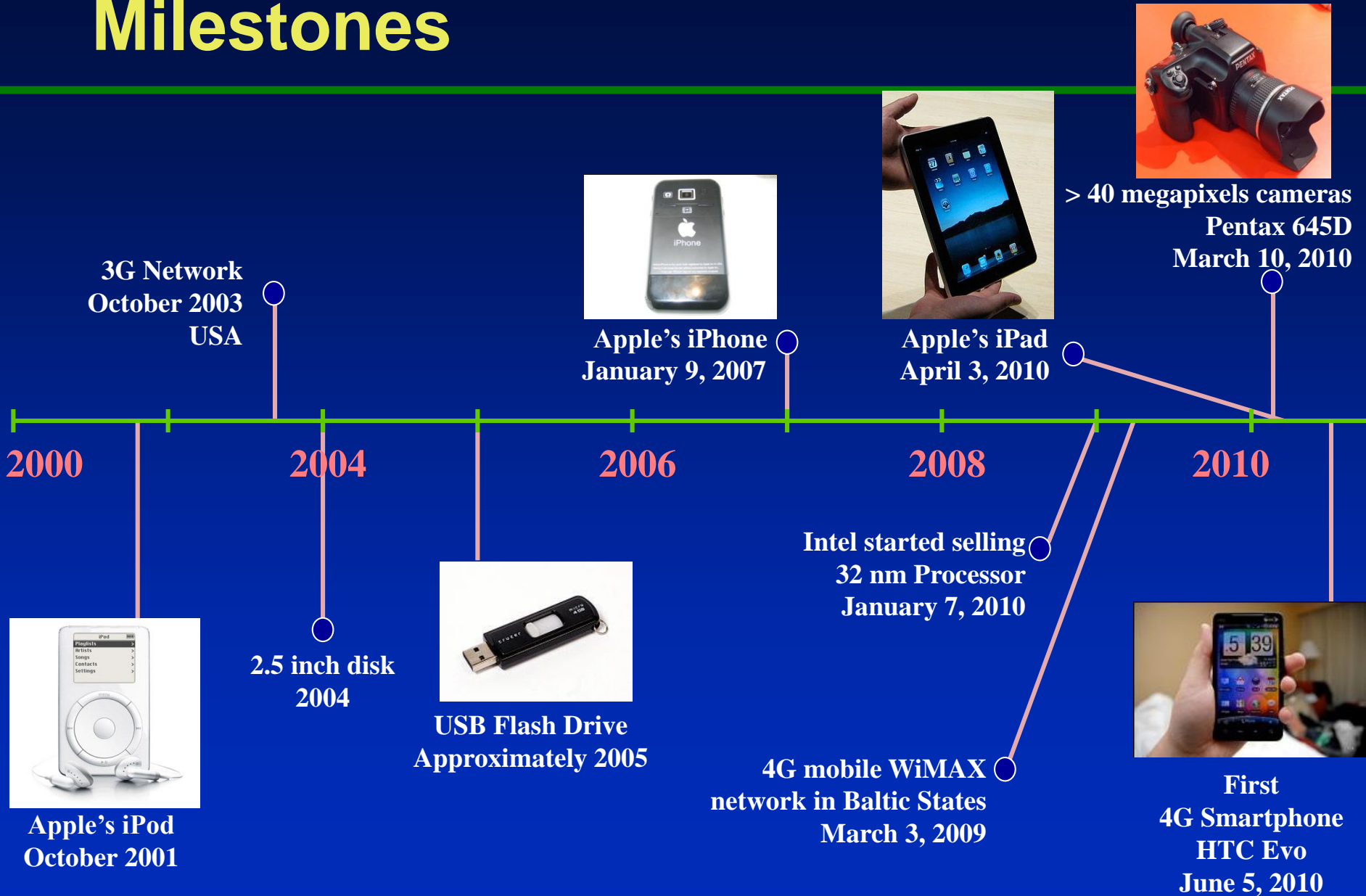
**D — Display Storage**

**V — Video**

# Computer Graphics Hardware Milestones



# Computer Graphics Hardware Milestones



Apple's iPod  
October 2001

3G Network  
October 2003  
USA

2.5 inch disk  
2004



USB Flash Drive  
Approximately 2005



Apple's iPhone  
January 9, 2007



Apple's iPad  
April 3, 2010

Intel started selling  
32 nm Processor  
January 7, 2010

4G mobile WiMAX  
network in Baltic States  
March 3, 2009

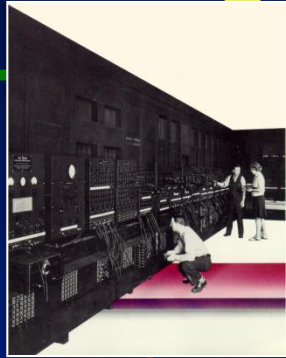


First  
4G Smartphone  
HTC Evo  
June 5, 2010



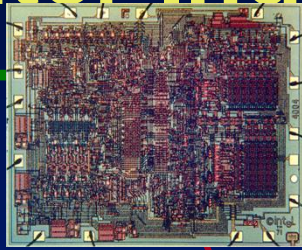
> 40 megapixels cameras  
Pentax 645D  
March 10, 2010

# Computer Industry Milestones



ENIAC  
1946

Acoustic  
Modem  
1966



Intel 4004  
1971



Apple II  
1977

Kodak  
DC420  
1995



Nikon  
Coolmax 950  
1999

NCSA  
Mosaic  
1993



1950

1960

1970

1980

1990

2000

Transistor  
1947



Mouse  
1968

ARPANET  
1969



DEC VAX  
11/780  
1978



Intel Pentium  
1993



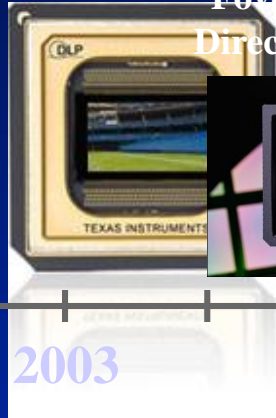
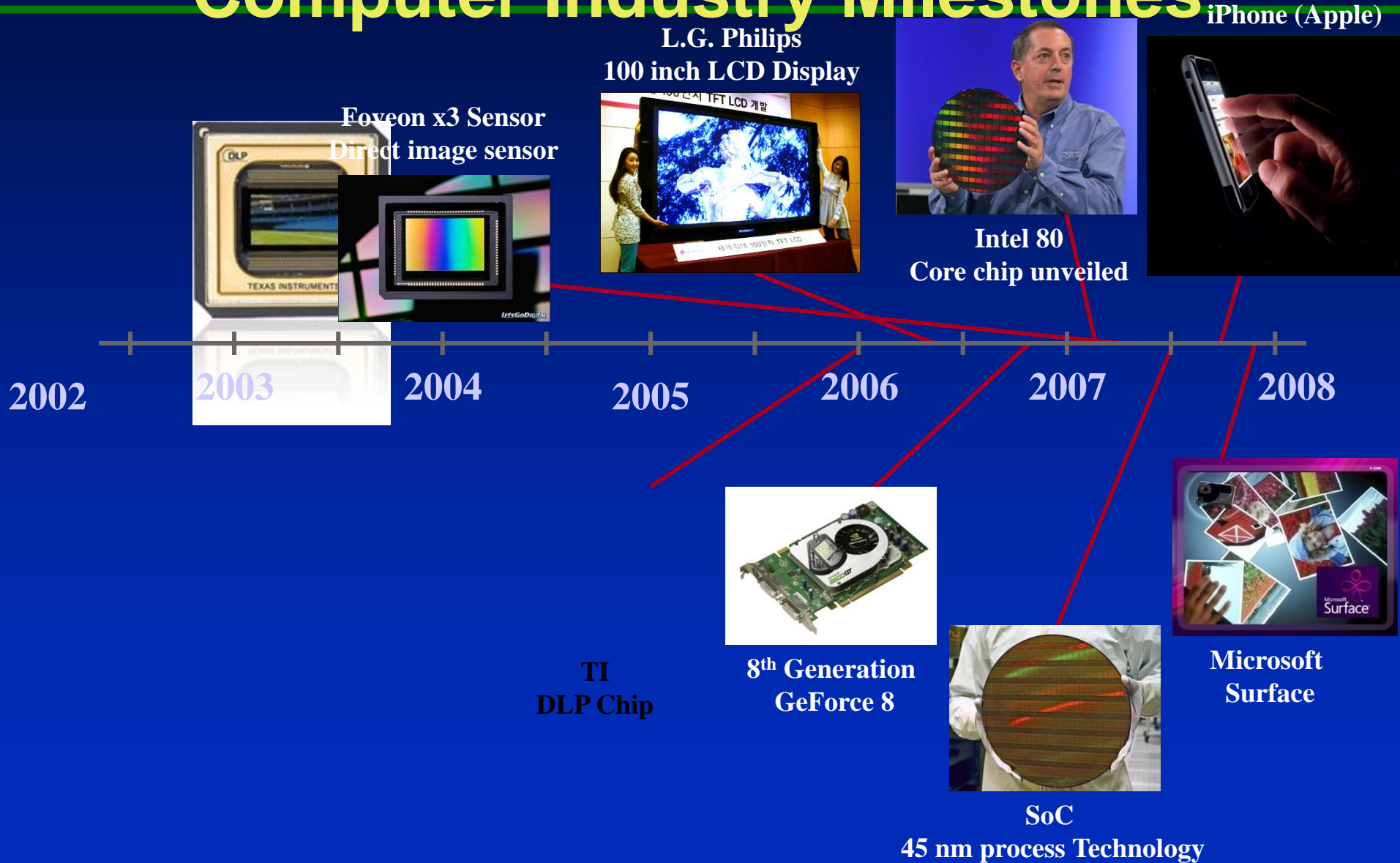
IBM PC  
1981



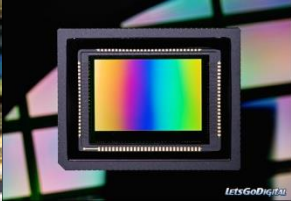
HP 610CL  
1999



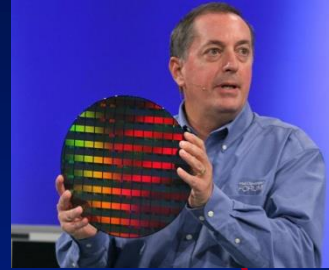
# Computer Industry Milestones



Foveon x3 Sensor  
Direct image sensor



L.G. Philips  
100 inch LCD Display



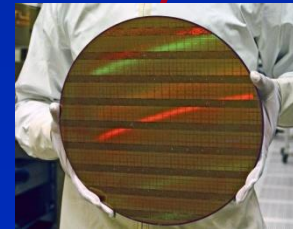
Intel 80  
Core chip unveiled



iPhone (Apple)



8th Generation  
GeForce 8

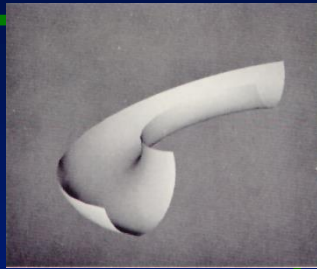


SoC  
45 nm process Technology



Microsoft  
Surface

# Computer Graphics Software Milestones



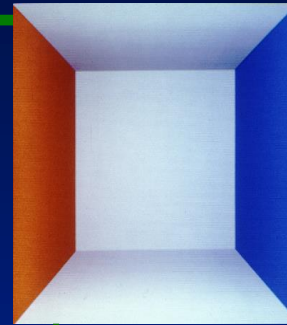
Gouraud Shading  
1971



Phong Shading  
1975



Cook-Torrance Model  
1981



Radiosity  
1984



Toy Story  
1995



1960

1970

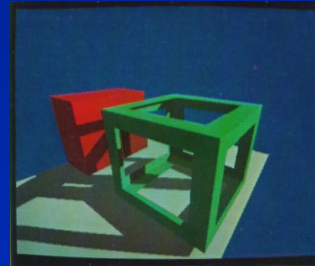
1980

1990

2000



Sketchpad  
1963



Ray Tracing  
1979

First Color Images in SIGGRAPH  
1977



He Model  
1991

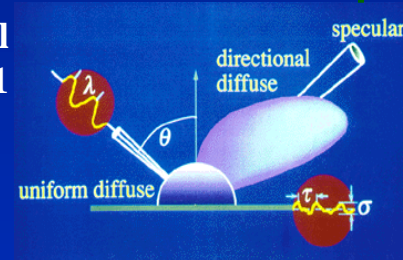
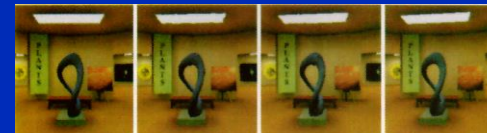


Image-Based Rendering  
1993

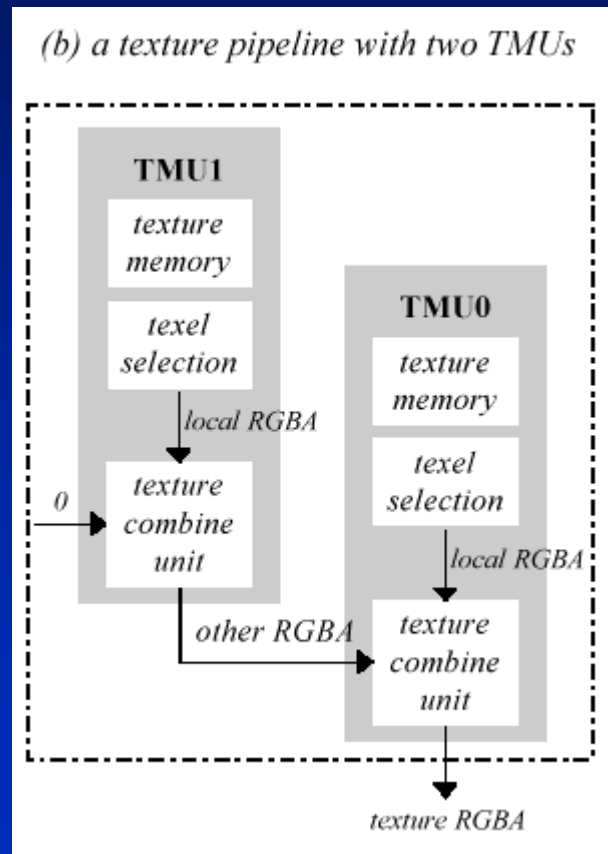


Light Field  
1996





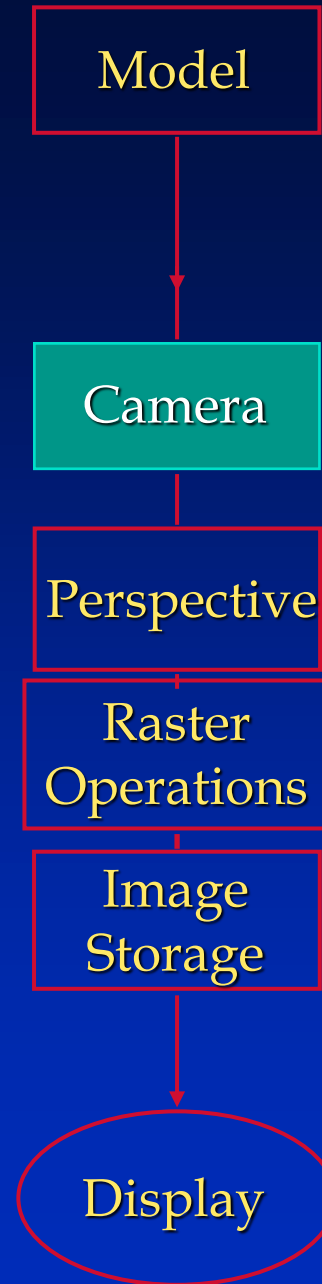
# Multitexturing



- Hardware architectures now support accessing more than one texture in a single pass

# Camera

- Viewer Position
- Viewer direction
- Field of view
  - Wide angle
  - Telephoto
- Depth of focus
  - Near
  - Far



# Model

- Environment

Geometry & topology

Material properties

>Color, reflectance, textures

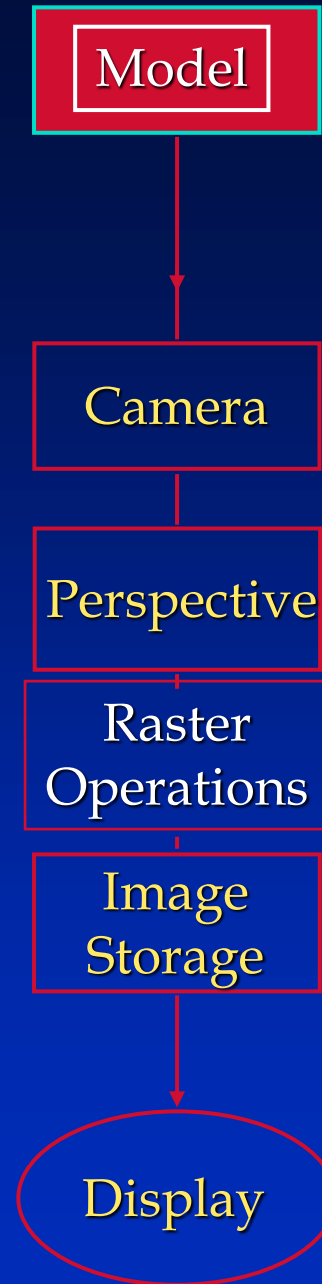
>(Cost, strength, thermal properties)

- Lighting

Geometry & position

Intensity, spectral distribution

Direction, spatial distribution



y ↑  
At a given scan-line,  $y$  is known.

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$$\text{Therefore, } ax + cz = -d - by$$

At a given pixel value of  $x$ ,  $x$  is also known

$$\text{Therefore, } z = \frac{-d - by - ax}{c}$$

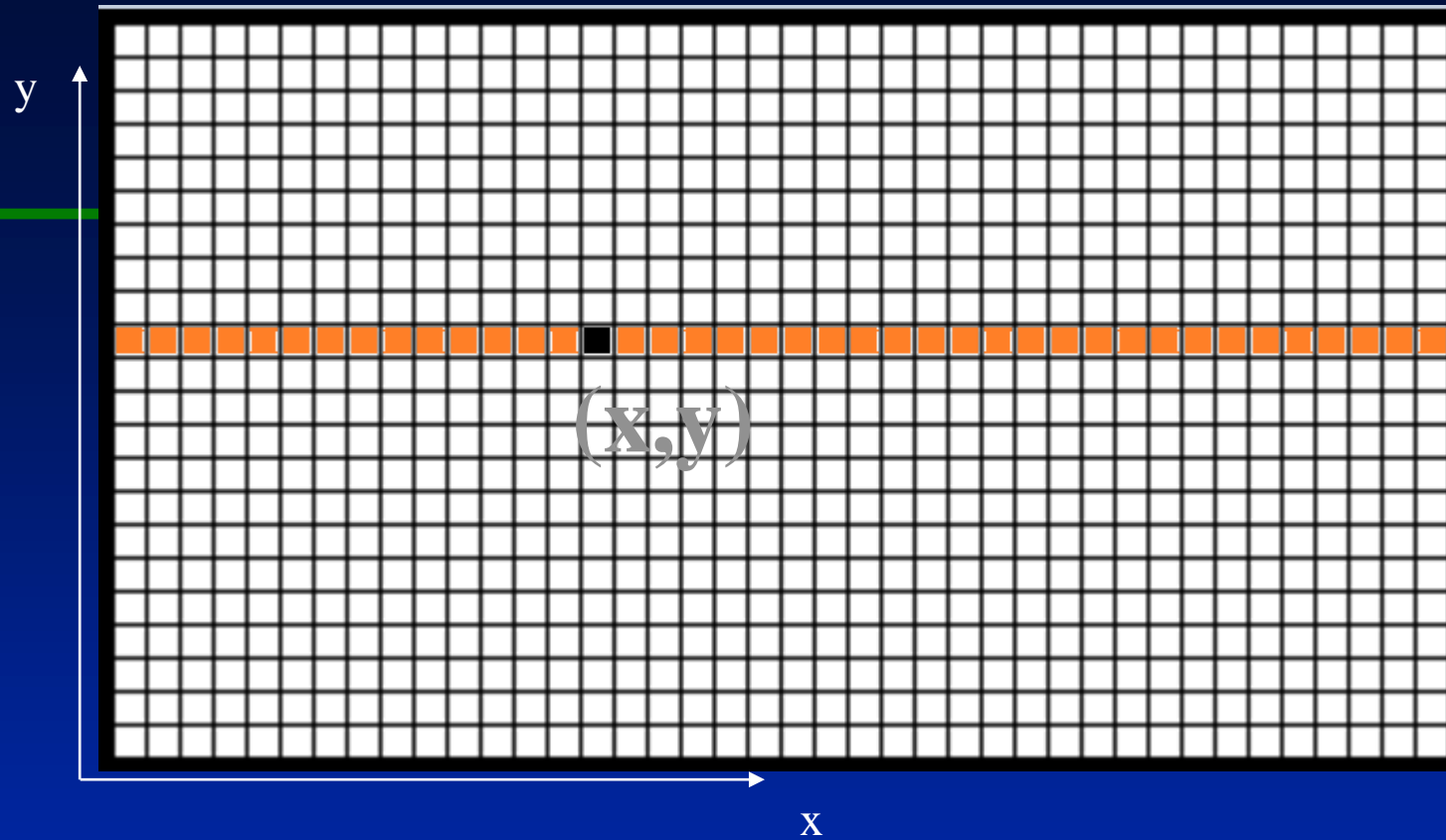
x →

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Planar equation of a polygon:

$$ax + by + cz + d = 0$$

where a, b, c, & d are constants

